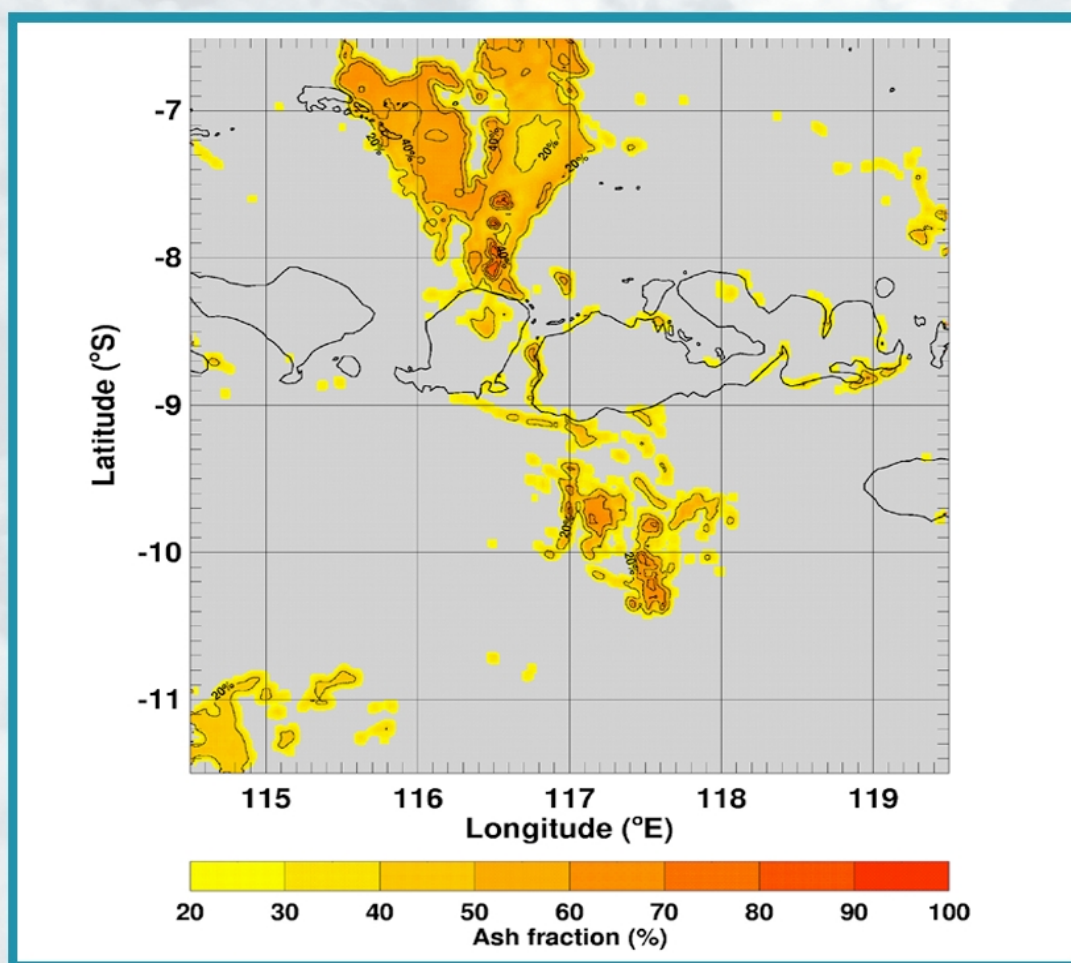


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## Determination of mass loadings and plume heights of volcanic ash clouds from satellite data.

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### Abstract

A retrieval scheme for determining some microphysical properties of volcanic ash clouds from thermal infrared satellite data is described. The mathematical details are provided here, while the broader implications of this research are outlined in a paper published by the *Quarterly Journal* (Prata and Grant, 2001). The report also provides details of the methods used to determine ash cloud heights from their shadows cast on land or ocean. The optical properties of a model andesite ash cloud are tabulated. These may be used in conjunction with data from advanced satellite sensors to infer ash cloud microphysics.

Radiative transfer (RT) calculations were also performed to investigate the relationship between top-of-the-atmosphere brightness temperatures (or radiances) in the split-window channels and water vapour amount for some current and planned satellite radiometers (e.g. AVHRR, ATSR-2, GMS-5 and GLI). The input data to the RT model come from the NCEP re-analysis and provide information on a spatial scale of  $2.5 \times 2.5$  degrees and temporal resolution of 6 hours.

Strong correlations were found between the difference in brightness temperatures (referred to as  $T_4 - T_5$ ) in the split-window channels and precipitable water, and between brightness temperature in one channel and precipitable water. Thus it follows that the relationship between the brightness temperature in one channel and the brightness temperature difference is a strong function of the precipitable water. Based on this, an empirical relationship is developed to describe the behaviour of  $T_4 - T_5$  as a function of  $T_4$  for global conditions. The relationship is then used to provide a water vapour correction for a modified volcanic ash detection scheme. The modified scheme retrieves the fraction of ash present in a pixel and is based on a simple model of the  $T_4 - T_5$  signature arising from ash and the empirical water vapour correction formula. Image-based estimates of the clear-sky, ash-free  $T_4 - T_5$ , the cloud-top temperature and the clear-sky surface temperature are required. Results using the modified scheme are shown for four test case eruptions.

## 1 Introduction

This report provides some mathematical details for determining mass loadings, plume heights and other cloud microphysical properties of volcanic ash clouds using satellite data. The report should be read in conjunction with a paper by the same authors published in the *Quarterly Journal of the Royal Meteorological Society* which provides the broader basis for this research, its context and usefulness to the aviation community. Apart from the more detailed mathematical descriptions provided here, some of the illustrations have been produced in colour, which aids in their interpretation, and there is an additional Table and some new results on a water vapour correction method.

The basic purpose of this research is to provide robust retrieval procedures for interpreting and quantitatively deriving microphysical properties of ash clouds. By understanding these properties it is hoped that operational procedures for the avoidance of hazardous volcanic ash clouds by aviation can be improved.

The report begins with a description of the radiative transfer procedures used to develop a retrieval scheme for deriving the particle sizes and mass loadings in volcanic ash clouds by utilising infrared radiation. The calculations are extended to cover the range of wavelengths likely to be available from existing or proposed satellite instruments. A tabulation of the optical parameters for this model is provided in this report.<sup>1</sup> The model is used to derive mass loadings for some eruptions from Mt. Ruapehu in New Zealand. Cloud height retrieval procedures are described next and a section is devoted to the mathematical details for the determination of cloud height from its shadow. The third part of the report includes a description of a new method for correcting infrared window radiances for the effects of water vapour. An illustration is given on how the method might work in practice using eruptions from Rindjani volcano in Indonesia.

## 2 Retrieval method

The radiative transfer required to extract quantitative information from infrared window radiances (8–12  $\mu\text{m}$ ) employs Mie theory and plane parallel radiative transfer in an absorbing and scattering cloud. Given the real and imaginary parts of the index of refraction of the ash-cloud particle as a function of wavelength, and the particle shape and size distribution, the efficiencies for scattering, absorption and extinction are calculated using a Mie scattering program. There is scant information on particle shapes in real ash clouds and only approximate methods exist for calculating efficiencies for particles of arbitrary shapes. We assume that the particles are spherical and the exact Mie-theory computer program of Evans (1988) is employed to calculate the efficiencies. Some measurements exist for the particle size distribution at the edges of the Mt. St. Helens ash cloud (see the papers in Newell and Deepak, 1982). These data indicate that a log-normal (or Zold) size distribution gives a reasonable fit to the distribution. The

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<sup>1</sup>A graphical presentation was given in the paper by Prata and Grant (2001).

measurements reported by King *et al.*, (1984) and Hoffman and Rosen (1984) of the El Chichón stratospheric aerosol layer fit a modified- $\gamma$  size distribution quite well. These data generally pertain to volcanic aerosol layers that are relatively old and high in the atmosphere. For this work, where only the fine particles can be detected in the nascent and low (tropospheric) volcanic plumes, we assume that the size distributions would be similar. We used both size distributions to perform the radiative transfer calculations, and although there were differences in detail between the results for the two distributions, the basic results and mass loadings were essentially the same.

The parameters used in the Mie program are described in Prata (1989b). Once the Mie program has been run for each value of the size parameter (mean particle size and monochromatic wavelength), scattering parameters are then fed into a plane-parallel discrete ordinates radiative transfer program (Stamnes and Swanson, 1981). Given the single scattering albedo, asymmetry parameter, extinction and scattering efficiencies as a function of monochromatic wavelength, and the cloud-top and surface temperatures, radiances emerging from the top of the cloud along  $n$  distinct streams (zenith angles) are computed. These radiances are calculated for cloud optical depths ranging from 0 to 20 at wavelengths corresponding to AVHRR-2 channels 4 and 5, and ATSR-2 11  $\mu\text{m}$  and 12  $\mu\text{m}$  channels. At the completion of these calculations, a large two-dimensional look-up table exists with entries at prescribed values of the mean particle size  $r_m$  and optical depth  $\tau$ . Each entry in the table consists of pairs of brightness temperatures  $T_4$  and  $T_5$ . The retrieval then consists of locating the  $(r_m, \tau)$  pairs within the look-up table that best match  $(T_4, T_5)$  pairs of AVHRR-2 or ATSR-2 measurements at each image pixel.

The calculations were performed assuming that there is no absorption of infrared radiation by water vapour. This is not correct, but the effect of water vapour absorption on the results is small for the volcanic plumes studied here. The effects of atmospheric water vapour absorption on the satellite brightness temperatures have been assessed by performing radiative transfer calculations. The radiative transfer model Modtran 3 (Berk *et al.*, 1989), was used to calculate the temperature difference between the the satellite measured brightness temperatures at 11  $\mu\text{m}$  and 12  $\mu\text{m}$  wavelengths, at each vertical level using the temperature and moisture structure from a nearby radiosonde profile. The results of this analysis are shown in Figure 3. The effect of water vapour is greatest at the lowest levels, where it exceeds 1 K. At higher levels, near to the location of the plume, the effect is less than 0.2 K. In the tropics and in high humidity conditions, the effect of water vapour absorption can mask out the ‘reverse’ absorption effect of volcanic ash clouds. This can lead to misidentification of volcanic clouds and is a limitation of the current thermal detection method.

## **Size distributions, scattering parameters and mass loading**

The modified- $\gamma$  distribution has the functional form,

$$n(r) = N_o \frac{r^\alpha}{\Gamma[\frac{\alpha+1}{\gamma}]} b^{\frac{\alpha+1}{\gamma}} \exp(-br^\gamma), \quad (1)$$

where  $n(r)$  is the number of particles per unit volume,  $r$  is the particle radius,  $\Gamma$  is the Gamma function (see Press *et al.*, 1986, page 156),  $N_o$ ,  $b$ ,  $\alpha$ , and  $\gamma$  are parameters of the distribution. The size parameter,  $x$ , is related to the particle radius and the wavelength  $\lambda$  through,

$$x = \frac{2\pi r}{\lambda}. \quad (2)$$

Used here,  $\gamma=1$ ,  $\alpha=6$ ,  $b = 6/r_o$ , and (6) reduces to,

$$n(x) = Cx^6 \exp\left(-\frac{6x}{x_o}\right),$$

where  $C$  is a constant replacing the other parameters. Within a distribution of sizes, the mode radius  $r_o$  corresponds to a mode size parameter  $x_o$ .

The log-normal distribution is described by,

$$n(x) = N_o \frac{1}{\sigma_x} \exp\left[-\frac{(\ln(x) - \ln(x_o))^2}{2\sigma_x^2}\right], \quad (3)$$

where, as before  $x$  is the size parameter. The parameter  $\sigma_x = 2\pi\sigma_r/\lambda$  is related to the standard deviation ( $\sigma_r$ ) of the distribution and is a measure of its spread. In the calculations performed with this distribution,  $\sigma_r$  was set to 0.5, 0.75, 1.0 and 1.25  $\mu\text{m}$ , and results are reported for  $\sigma_r=1.0 \mu\text{m}$ .

The inputs to the Mie program are the real and imaginary parts of the refractive index ( $m$ ), the size parameter and the size distribution. The outputs are the extinction efficiency ( $\hat{Q}_{ext}$ ) and scattering efficiency ( $\hat{Q}_{sca}$ ) and phase function ( $P(\theta)$ ). For polydispersions these efficiency factors are related to the single particle efficiencies ( $Q_f$ ) by,

$$\hat{Q}_f = \frac{\int_0^\infty \pi r^2 Q_f\left(\frac{2\pi r}{\lambda}, m\right) \frac{dn(r)}{dr} dr}{\int_0^\infty \pi r^2 \frac{dn(r)}{dr} dr}. \quad (4)$$

The absorption efficiency is,

$$\hat{Q}_{abs} = \hat{Q}_{ext} - \hat{Q}_{sca}. \quad (5)$$

The remaining parameters that are needed to perform the radiative transfer calculations and which relate to the cloud microphysical structure are: The single scattering albedo,

$$\varpi = \frac{\hat{Q}_{ext}}{\hat{Q}_{sca}}, \quad (6)$$

the asymmetry parameter,

$$g = \frac{1}{2} \int_{-1}^1 P(\theta) \cos \theta d \cos \theta, \quad (7)$$

where  $\theta$  is the scattering angle. The number of particles per unit volume in the cloud is,

$$N = \int_0^\infty \frac{dn}{dr} dr, \quad (8)$$

and the optical depth of the cloud is,

$$\tau_\lambda = \pi L \int_0^\infty r^2 Q_{ext}(r, \lambda) n(r) dr, \quad (9)$$

where  $L$  is the geometrical thickness of the cloud. The mass loading ( $\text{kg m}^{-3}$ ) is

$$M = \frac{4\pi}{3} \rho \int_0^\infty r^3 n(r) dr, \quad (10)$$

where  $\rho$  is the density of the ash. The total mass can be calculated by multiplying (15) by the volume of a pixel (geometric thickness multiplied by the area of a pixel).

## Retrieval procedure

In the  $(T_4, T_4 - T_5)$  plane there exist isolines of constant mean particle radius,  $r_m^j$ . Each point on the isoline,  $r_m^j$  corresponds to particular values of the optical depth,  $\tau^{j,i}$ . Lines connecting equal values of  $\tau^{j,i}$  also exist. Given the measured values  $(T_4^*, T_5^*)$ , the retrieval procedure requires us to find the ‘best’ values of  $(\tau, r_m)$ . A linear interpolation procedure is adopted:

- Find values of  $T_4(\tau^{j,i}, r_m^j)$  that bracket  $T_4^*$ . Label these  $T_4^1(r_m^j), T_4^2(r_m^j), T_4^1(r_m^{j+1}), T_4^2(r_m^{j+1})$
- Interpolate on the  $r_m^j$  isolines to find the appropriate  $\Delta T(r_m^j) (= T_4(r_m^j) - T_5(r_m^j))$ .

$$\Delta T(r_m^j) = w_1 \Delta T_2(r_m^j) + (1 - w_1) \Delta T_1(r_m^j),$$

$$w_1 = \frac{T_4^1(r_m^j) - T_4^*}{T_4^1(r_m^j) - T_4^2(r_m^j)}.$$

Similarly for  $\Delta T(r_m^{j+1})$ :

$$\Delta T(r_m^{j+1}) = w_2 \Delta T_2(r_m^{j+1}) + (1 - w_2) \Delta T_1(r_m^{j+1}),$$

and the weight  $w_2$  is defined in an analogous way to  $w_1$ .

- The required mean particle radius is obtained using linear interpolation,

$$r_m^* = w_r r_m^j + (1 - w_r) r_m^{j+1},$$

$$w_r = \frac{\Delta T(r_m^{j+1}) - \Delta T^*}{\Delta T(r_m^{j+1}) - \Delta T(r_m^j)}.$$

- In practice there are  $n$  isolines of  $r_m^j, j = 1, n$  and  $n$  is small ( $n = 18$ ), and many more values of  $\tau^{j,i}, i = 1, k$  ( $k = 100$  is used in the current software). Thus  $2n \times k$  values of  $\Delta T$  are precomputed.

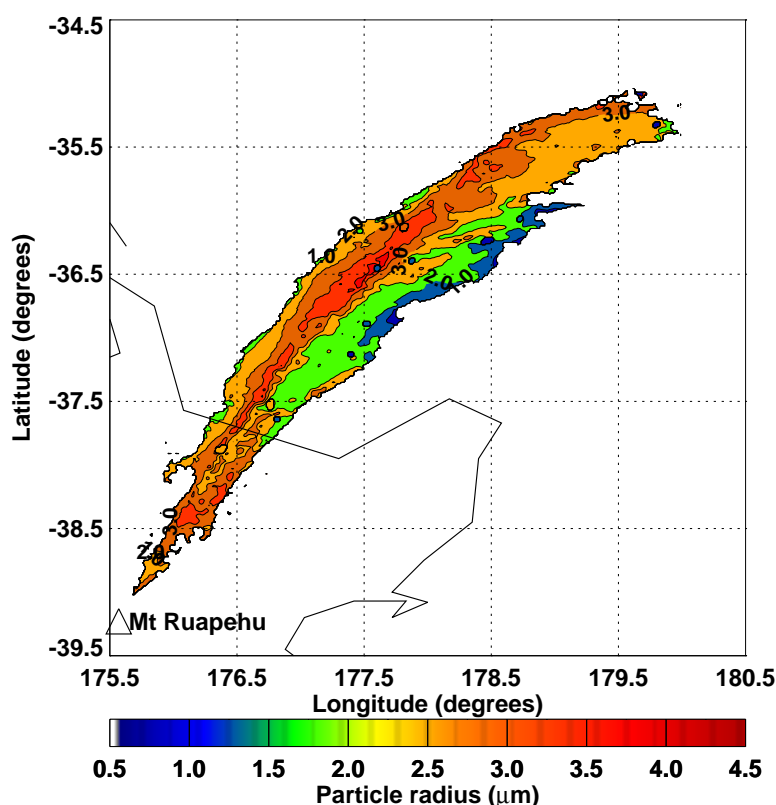


Figure 4. Particle size retrieval for the eruption of 17 June 1996 using AVHRR-2 data.

### 3 Particle radius retrievals

Figure 4 shows a contour plot of mean particle radius retrieved from the AVHRR-2 image shown in Figure 1(a). The largest particles (up to  $\approx 4 \mu\text{m}$  radii) are found around the middle of the plume and in ‘clumps’ distributed non-uniformly along the plume. Some large particles found at the edges may be an artifact of the analysis because these regions are quite transparent and as explained previously it is possible that the entrainment of ambient (water-rich) air may be significant. There are, however, closed contours within the plume with congregations of large particles. There appears to be an elongation of the particle size contours in the direction of the wind at that level. There also appears to be a gradient in particle size from smallest particles in the southeastern side of the plume, to largest particles in the northwestern side of the plume.

Figure 5 shows the frequency distribution of particle sizes in the plumes for both size distribution models. Particle sizes vary from  $1 \mu\text{m}$  up to  $\approx 4 \mu\text{m}$ , with mode maxima near  $3 \mu\text{m}$ . There is some evidence of multiple modes within the distribution and such behaviour has been found for the Fuego and Santiago ash clouds (Cadle *et al.*, 1979), the Mt. St. Helens ash cloud (Chuan *et al.*, 1981; Farlow *et al.*, 1981), and the Agung ash clouds (Mossop, 1964). Chuan *et al.* (1981) found a mode peak at radius  $\approx 2.5 \mu\text{m}$  from monitoring continuous emissions from Mt. St. Helens, prior to a strong eruption on August 7 1980.



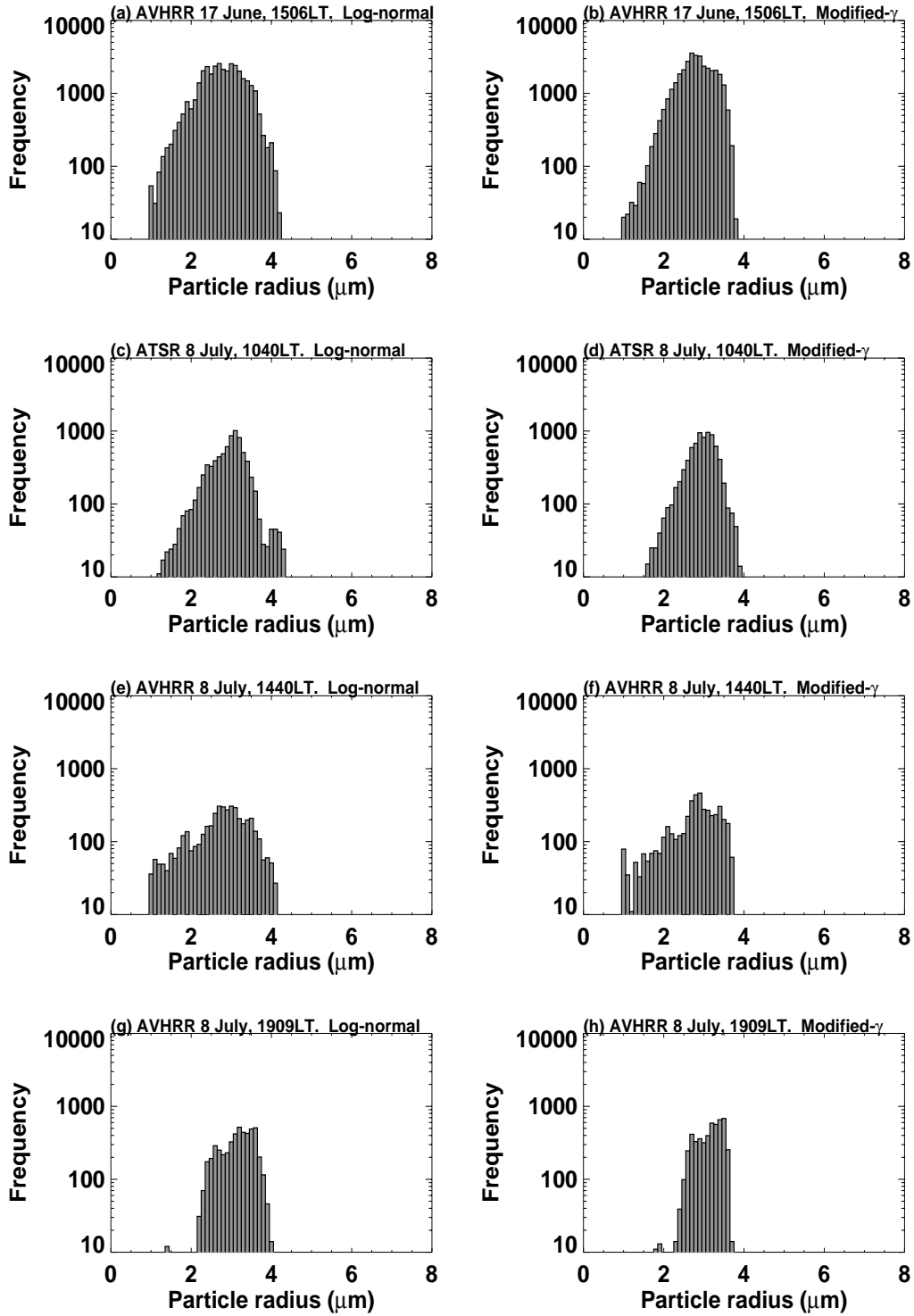


Figure 5. Retrieved particle size histograms for four Ruapehu plumes and two model size distributions.

## 4 Mass loadings

The U. S. Military consider mass loadings  $> 50 \text{ mg m}^{-3}$  a potential hazard to their aircraft operations. Przedpelski and Casadevall (1994) estimated a mass loading of  $\approx 2000 \text{ mg m}^{-3}$  at 25,000 ft ( $\approx 7.5 \text{ km}$ ) for the 15 December 1989 Redoubt eruption cloud that caused significant damage to a KLM Boeing 747-400 jet aircraft. Mass loadings include all particles with radii  $< 50 \mu\text{m}$ , which have atmospheric residence times of the order of at least a few hours. Having determined the particle size distribution, the geometrical thickness of the cloud and its areal extent, it is possible to estimate the mass loading of fine particles in each of the plumes studied here. The density of the ash is taken to be  $2600 \text{ kg m}^{-3}$  and the area of a pixel is taken as  $1.2 \times 1.2 \text{ km}^2$  – this is a mean area for pixels for both the AVHRR-2 and ATSR-2. Pixels are counted if they satisfy criterion (1), and the retrieved particle size is in the range  $1 < r_m < 8 \mu\text{m}$ . An estimate of the cloud thickness is crucial to the evaluation of mass loadings. Data on cloud thicknesses are not available so they must be estimated by other means. Studies of plume rise in stable stratified atmospheres (e.g. Briggs, 1975) suggest that to a reasonable approximation the vertical extent of a plume can be estimated from the cloud-top height. For example, Manins (1985) has calculated the heights and vertical extents of stabilized smoke plumes as a function of power release and following Briggs (1975) suggests that the vertical extent (cloud thickness),  $\Delta z$ , of these plumes is given by,

$$\Delta z = 0.4z_{top},$$

where  $z_{top}$  is the height of the plume top. The cloud-top heights calculated previously for the Ruapehu plumes suggest a cloud thickness range of 1.5–3.0 km, with a likely error of  $\pm 0.5 \text{ km}$ . The variability of cloud thickness along the plumes and the problem of not having simultaneous plume-top height and plume-base height data for each of the plumes, means that we cannot estimate plume thickness to any greater accuracy. The mass loading ( $\text{kg m}^{-3}$ ) is

$$M = \frac{4\pi}{3} \rho \int_0^\infty r^3 n(r) dr, \quad (11)$$

where  $\rho$  is the density of the ash and  $n(r)$  is the size distribution. The total mass can be calculated by multiplying (6) by the volume of a pixel (geometric thickness multiplied by the area of a pixel). Table 1 lists the results obtained for all four plumes using both size distributions.

Table 1: Retrieved mass loadings and mode radii for the two size distributions used and for four Ruapehu plumes. The range of mass loadings shown corresponds to a range in cloud thickness from 1.5 km to 3.0 km.

Date:Time	Sensor	Size distribution			
		Log-normal		Modified- $\gamma$	
		Mass loading ( $\text{mg m}^{-3}$ )	Mode radius ( $\mu\text{m}$ )	Mass loading ( $\text{mg m}^{-3}$ )	Mode radius ( $\mu\text{m}$ )
17-06-96:1506	AVHRR-2	3.5–6.9	2.7	3.2–6.3	2.7
08-07-96:1040	ATSR-2	1.4–2.7	3.1	1.4–2.6	3.1
08-07-96:1440	AVHRR-2	1.5–2.9	3.0	1.4–2.6	2.9
08-07-96:1909	AVHRR-2	1.7–3.2	3.2	1.5–2.9	3.5

The retrievals for the 8 July plumes should be comparable, as the time difference between the AVHRR-2 and ATSR-2 data acquisitions is not long (less than five hours) and the eruptions during these days were similar in nature. The mode radii on all days are similar, but the mass loading differences between the June eruption and the July events are probably significant.

Hobbs *et al.* (1981) made aircraft-based measurements of the size distributions and number densities of ash in the periphery of the Mt. St. Helens plume. Some measurements were made at 3 km altitude and 9.3 km downwind of the volcano and these can be compared with our results. For particles in the size range 1–5  $\mu\text{m}$ , the number density is of the order 10–1  $\text{cm}^{-3}$  (see Fig. 2B of Hobbs *et al.*, 1981), which correspond to mass loadings of 0.1–1.0  $\text{mg m}^{-3}$ . Sehmel (1982) also reported mass loadings in the range 1–10  $\text{mg m}^{-3}$  in the dispersed Mt. St. Helens volcanic cloud. Our results may also be compared with silicate mass loading retrievals by Yu and Rose (1999) for the El Chichón clouds, and from recent estimates made by W. I. Rose for the June - September 1992 Spurr eruptions (personal communication). These mass loadings were found to be in the range 1–5  $\text{mg m}^{-3}$ . Wen and Rose (1994) determined the total mass of fine particles for the August 19 1992 Crater Peak/Spurr eruption and obtained a value of  $0.2 \times 10^6$  t. They estimated the cloud area to be  $10^5$   $\text{km}^2$ , giving a mass loading range of 1.5–3.0  $\text{mg m}^{-3}$  for a cloud thickness range of 1.5–3.0 km. Wen and Rose also show that their total mass estimates are not significantly affected by the choice of size distribution.

The mean retrieved mass loadings are an order of magnitude smaller than the value considered hazardous to aircraft (cf.  $\approx 50$   $\text{mg m}^{-3}$  or greater). The mass loadings calculated here represent only those particles in the restricted size range,  $1 < r < 8$   $\mu\text{m}$ , and these represent only a small fraction of the total mass of ejected matter. However, these are the particles which are most hazardous to jet engines and it would appear to be necessary to develop a mass loading threshold based on particles in this size range. The mass in this size range typically represents  $\approx 1\%$  of the total mass ejected (e.g. Wen and Rose, 1994; Bursik *et al.*, 1994), which suggests a *total* mass loading of 100–500  $\text{mg m}^{-3}$  for the Ruapehu clouds and thus they would have been a threat to jet aircraft.

## **5 Volcanic cloud model**

The new (e.g. MODIS) and proposed advanced multispectral sensors (e.g. GLI, SEVIRI) include many channels capable of providing detection and discrimination of volcanic ash clouds. A model of an ash cloud has been developed in order to exploit these new sensors. We include information from the visible to infrared—although most of the discussion has centred on the infrared window radiances, it seems likely that the visible and near infrared data may also provide a means for ash cloud detection.

At near infrared wavelengths (e.g.  $\lambda=1.61$   $\mu\text{m}$ ) ice clouds appear much darker than clouds of water droplets, because the imaginary part of the refractive index of ice is larger than that of water at this wavelength and consequently ice absorbs more strongly at this wavelength. A comparison of the refractive indices of water, ice and andesite (a common constituent of ash clouds) is given in Table 2.

Table 2: Refractive indices for water, ice and andesite (a silica-rich mineral). The last column gives the reference to the origin of the data shown.

Wavelength ( $\mu\text{m}$ )	$n_r$	$n_i$	Reference
<i>Ice</i>			
0.63	1.309	1.04E-8	Masuda and Takashima (1990)
1.61	1.289	3.41E-4	Masuda and Takashima (1990)
<i>Water</i>			
0.63	1.332	1.44E-8	Masuda and Takashima (1990)
1.61	1.317	0.87E-4	Masuda and Takashima (1990)
<i>Andesite</i>			
0.68	1.470	1.70E-3	Pollack <i>et al.</i> (1973)
1.61	1.470	3.30E-3	Pollack <i>et al.</i> (1973)

Pollack *et al.* (1973) list refractive indices of andesite (and some other minerals) over a large range of wavelengths from the UV to the infrared. These data are not the only source of refractive index values for minerals; see for example, Volz (1973), Ivlev and Popova (1973) and Sokolik and Toon (1999). We have used the Pollack *et al.* values as a starting point to provide the input optical parameters required for more detailed radiative transfer calculations, and we propose a model of a volcanic ash cloud based on the Pollack *et al.* refractive indices of andesite. The ash cloud model consists of spherical andesite particles in a log-normal size distribution with a mean particle radius of  $3 \mu\text{m}$ . The single-scatter albedo, asymmetry parameter and coefficients of absorption, scattering and extinction are calculated for the polydisperse particle size distribution using the Mie program discussed earlier. Table 3 provides a listing of the variation of single-scatter albedo ( $\varpi$ ), extinction coefficient ( $Q_{ext}$ ), and asymmetry parameter ( $g$ ) for wavelengths ranging from  $0.3 \mu\text{m}$  to  $14.5 \mu\text{m}$ —the range most commonly used in remote sensing of the earth’s atmosphere. Also, shown are the results for a model ash cloud with mean particle radii of 1 and  $5 \mu\text{m}$ .

Table 3: Optical parameters for a model andesite ash cloud. The parameters are:  $\varpi$ —the single-scatter albedo,  $g$ — the asymmetry parameter, and  $Q_{ext}$ —the extinction efficiency factor. These parameters are given for three mean particle sizes,  $r_o=1, 3$  and  $5 \mu\text{m}$ .

Wavelength ( $\mu\text{m}$ )	$r_o=1.0 \mu\text{m}$			$r_o=3.0 \mu\text{m}$			$r_o=5.0 \mu\text{m}$		
	$\varpi$	$g$	$Q_{ext}$	$\varpi$	$g$	$Q_{ext}$	$\varpi$	$g$	$Q_{ext}$
0.30	0.8346	0.4579	2.0875	0.8344	0.4573	2.0873	0.8343	0.4570	2.0872
0.32	0.8241	0.4551	2.0875	0.8238	0.4543	2.0873	0.8237	0.4540	2.0872
0.34	0.8229	0.4548	2.0876	0.8225	0.4540	2.0873	0.8224	0.4536	2.0872
0.36	0.8104	0.4513	2.0876	0.8100	0.4503	2.0873	0.8098	0.4499	2.0872
0.38	0.8105	0.4515	2.0877	0.8100	0.4504	2.0873	0.8098	0.4499	2.0872
0.40	0.7987	0.4480	2.0877	0.7982	0.4467	2.0873	0.7980	0.4462	2.0872
0.42	0.7988	0.4482	2.0878	0.7982	0.4469	2.0874	0.7980	0.4462	2.0872
0.44	0.7877	0.4448	2.0879	0.7871	0.4433	2.0874	0.7868	0.4426	2.0872
0.46	0.7878	0.4451	2.0880	0.7871	0.4434	2.0874	0.7868	0.4427	2.0872
0.48	0.7879	0.4454	2.0880	0.7872	0.4436	2.0875	0.7868	0.4428	2.0872
0.50	0.7775	0.4421	2.0881	0.7766	0.4401	2.0875	0.7762	0.4392	2.0872
0.52	0.7776	0.4424	2.0882	0.7767	0.4403	2.0876	0.7763	0.4393	2.0872
0.54	0.7778	0.4428	2.0883	0.7768	0.4405	2.0876	0.7763	0.4394	2.0873
0.56	0.7679	0.4396	2.0884	0.7668	0.4371	2.0876	0.7663	0.4359	2.0873
0.58	0.7681	0.4400	2.0886	0.7669	0.4373	2.0877	0.7663	0.4361	2.0873
0.60	0.7683	0.4405	2.0887	0.7670	0.4376	2.0878	0.7664	0.4362	2.0874
0.70	0.7509	0.4363	2.0894	0.7490	0.4321	2.0881	0.7482	0.4302	2.0875
0.80	0.7357	0.4331	2.0903	0.7331	0.4274	2.0886	0.7320	0.4248	2.0878
0.90	0.7225	0.4313	2.0914	0.7191	0.4236	2.0892	0.7176	0.4202	2.0882
1.00	0.7112	0.4308	2.0928	0.7067	0.4209	2.0899	0.7048	0.4165	2.0887
1.10	0.7016	0.4319	2.0945	0.6960	0.4192	2.0908	0.6935	0.4136	2.0892
1.20	0.6937	0.4346	2.0966	0.6866	0.4186	2.0918	0.6836	0.4118	2.0899
1.30	0.6873	0.4392	2.0991	0.6786	0.4193	2.0931	0.6749	0.4109	2.0908
1.40	0.6871	0.4476	2.1021	0.6763	0.4234	2.0945	0.6720	0.4132	2.0917
1.50	0.6834	0.4562	2.1057	0.6702	0.4266	2.0963	0.6651	0.4144	2.0929
1.60	0.6853	0.4685	2.1101	0.6694	0.4331	2.0983	0.6632	0.4185	2.0942
1.70	0.6883	0.4830	2.1155	0.6691	0.4408	2.1007	0.6619	0.4236	2.0957
1.80	0.6926	0.4998	2.1219	0.6695	0.4499	2.1034	0.6610	0.4298	2.0975
1.90	0.6983	0.5189	2.1298	0.6706	0.4605	2.1066	0.6607	0.4371	2.0995
2.00	0.7019	0.5411	2.1395	0.6688	0.4728	2.1104	0.6572	0.4454	2.1019
2.10	0.7143	0.5655	2.1511	0.6749	0.4880	2.1148	0.6614	0.4565	2.1046
2.20	0.7248	0.5909	2.1651	0.6785	0.5038	2.1199	0.6627	0.4677	2.1076
2.30	0.7369	0.6174	2.1817	0.6829	0.5213	2.1258	0.6647	0.4803	2.1110
2.40	0.7507	0.6441	2.2014	0.6882	0.5406	2.1326	0.6672	0.4944	2.1150
2.50	0.7686	0.6699	2.2242	0.6977	0.5621	2.1404	0.6736	0.5109	2.1195
2.55	0.7750	0.6821	2.2369	0.6996	0.5727	2.1448	0.6739	0.5188	2.1219
2.60	0.7845	0.6935	2.2503	0.7049	0.5843	2.1494	0.6775	0.5279	2.1245
2.65	0.7885	0.7045	2.2645	0.7043	0.5953	2.1544	0.6752	0.5361	2.1273
2.70	0.7955	0.7145	2.2795	0.7072	0.6070	2.1597	0.6762	0.5453	2.1302
2.75	0.7931	0.7249	2.2949	0.6996	0.6183	2.1653	0.6670	0.5533	2.1333
2.80	0.7961	0.7338	2.3110	0.6983	0.6306	2.1712	0.6639	0.5630	2.1366
2.85	0.8037	0.7407	2.3277	0.7022	0.6432	2.1776	0.6659	0.5738	2.1401
2.90	0.8091	0.7468	2.3448	0.7040	0.6559	2.1843	0.6658	0.5847	2.1437
2.95	0.8185	0.7507	2.3623	0.7106	0.6682	2.1914	0.6703	0.5963	2.1476
3.00	0.8275	0.7534	2.3800	0.7173	0.6802	2.1988	0.6750	0.6080	2.1517
3.05	0.8381	0.7545	2.3980	0.7265	0.6917	2.2067	0.6821	0.6198	2.1560
3.10	0.8464	0.7549	2.4158	0.7334	0.7028	2.2149	0.6871	0.6316	2.1605
3.15	0.8543	0.7544	2.4335	0.7404	0.7133	2.2235	0.6923	0.6433	2.1653
3.20	0.8635	0.7526	2.4511	0.7498	0.7229	2.2324	0.7000	0.6550	2.1702
3.25	0.8688	0.7511	2.4682	0.7546	0.7325	2.2416	0.7030	0.6666	2.1754
3.30	0.8739	0.7489	2.4848	0.7593	0.7414	2.2512	0.7062	0.6781	2.1807
3.35	0.8803	0.7458	2.5009	0.7664	0.7491	2.2611	0.7118	0.6892	2.1863
3.40	0.8862	0.7423	2.5163	0.7733	0.7560	2.2713	0.7174	0.7000	2.1920
3.45	0.8904	0.7390	2.5308	0.7779	0.7625	2.2817	0.7208	0.7107	2.1980
3.50	0.8943	0.7355	2.5444	0.7825	0.7682	2.2924	0.7242	0.7210	2.2041
3.60	0.9014	0.7281	2.5686	0.7915	0.7773	2.3146	0.7312	0.7403	2.2168
3.70	0.9101	0.7198	2.5882	0.8041	0.7821	2.3376	0.7427	0.7565	2.2302
3.80	0.9166	0.7120	2.6023	0.8140	0.7846	2.3614	0.7518	0.7706	2.2442
3.90	0.9233	0.7042	2.6105	0.8252	0.7842	2.3859	0.7628	0.7815	2.2586
4.00	0.9277	0.7108	2.5773	0.8341	0.7921	2.4195	0.7706	0.7975	2.2773
4.25	0.9352	0.6941	2.5293	0.8494	0.7846	2.4868	0.7858	0.8109	2.3174
4.50	0.9402	0.6765	2.4326	0.8623	0.7737	2.5565	0.7991	0.8122	2.3595
4.75	0.9432	0.6564	2.2915	0.8733	0.7630	2.6272	0.8107	0.8060	2.4037
5.00	0.9413	0.6419	1.9900	0.8819	0.7704	2.6963	0.8184	0.8058	2.4602
5.25	0.9389	0.6130	1.7826	0.8875	0.7668	2.7580	0.8242	0.7977	2.5105
5.50	0.9363	0.5811	1.5711	0.8942	0.7646	2.8121	0.8322	0.7894	2.5637
5.75	0.9300	0.5473	1.3668	0.8966	0.7648	2.8536	0.8351	0.7841	2.6194
6.00	0.9101	0.5133	0.9693	0.9004	0.7970	2.7883	0.8464	0.8093	2.7209
6.50	0.8380	0.4382	0.5776	0.8790	0.8161	2.5113	0.8356	0.8449	2.8205
7.00	0.6549	0.3645	0.3470	0.8058	0.8202	1.9370	0.7889	0.8848	2.6700
7.50	0.3096	0.2950	0.2404	0.5937	0.8105	1.1636	0.6491	0.9068	1.9243
8.00	0.0625	0.2346	0.2882	0.2155	0.7863	0.8026	0.3052	0.9043	1.1673
8.25	0.0655	0.2090	0.4060	0.2279	0.7644	0.9701	0.3203	0.8907	1.3045
8.50	0.1075	0.1876	0.6204	0.3284	0.7318	1.3266	0.4219	0.8611	1.6615
8.75	0.1541	0.1706	1.0082	0.4087	0.6886	1.7910	0.4909	0.8110	2.0317
9.00	0.2049	0.1552	1.7692	0.4686	0.6440	2.3946	0.5405	0.7500	2.4372
9.50	0.1948	0.1366	1.7248	0.4238	0.6592	2.5902	0.4845	0.7775	2.5805
10.00	0.2305	0.1146	1.7813	0.4522	0.6202	2.8094	0.5021	0.7457	2.7180
10.50	0.2495	0.1181	1.3480	0.4546	0.6133	2.8707	0.4883	0.7495	2.7459
11.00	0.3553	0.1286	0.8027	0.5088	0.5991	3.1600	0.4782	0.7452	2.8292
11.50	0.4019	0.0997	0.4043	0.6265	0.5784	3.2195	0.5362	0.7079	3.0643
12.00	0.3958	0.0778	0.2422	0.6997	0.5613	2.8904	0.6367	0.6834	3.3369
12.50	0.3572	0.0625	0.1627	0.7302	0.5433	2.4190	0.7080	0.6870	3.4567
13.00	0.2762	0.0515	0.1285	0.7139	0.5216	1.9619	0.7268	0.7007	3.3357
13.50	0.1904	0.0433	0.1110	0.6736	0.4931	1.5435	0.7210	0.7084	3.0193
14.00	0.1153	0.0377	0.1134	0.5966	0.4607	1.2558	0.6783	0.7107	2.6238

## 6 Cloud height determination

### Cloud-top temperature/temperature profile method

Cloud-top height can be determined by using the cloud-top temperature of opaque parts of the cloud as a proxy for the ambient temperature at the same height as the cloud top. A nearby radiosonde profile is then used to determine the height in the profile where the temperature best matches the cloud-top temperature. This method can work well provided the cloud behaves as a blackbody and the radiosonde profile is representative. For high clouds near the tropopause, the method is prone to error because the rate of change of temperature with height is small and this leads to indeterminacy in the height assignment.

Figure 6 shows an AVHRR-2 image of the volcanic ash plume on 17 June 1996. The plume is shown as the 11  $\mu\text{m}$  brightness temperature (AVHRR-2 channel 4) overlayed on the near infrared (AVHRR-2 channel 2) image. The plume was highlighted by selecting only those regions for which  $T_4 - T_5 < +0.5$  K. The coldest parts of the plume (coloured blue) have temperatures in the range  $-32^\circ\text{C}$  to  $-38^\circ\text{C}$ . It is reasonable to expect that the cloud is not black (see, for example Platt and Stephens, 1984), so the air temperature at the top of the cloud might be expected to be a few K lower. The four locations marked on the image correspond to thick cloud (A), semi-transparent cloud (B), clear sea surface (C), and clear land surface (D). The 11  $\mu\text{m}$  brightness temperatures corresponding to these locations are:  $-37^\circ\text{C}$  (A),  $-4.2^\circ\text{C}$  (B),  $12.8^\circ\text{C}$  (C), and  $7.3^\circ\text{C}$  (D).

Radiosonde data were obtained from the Crown Research Institute, New Zealand (Burgess, personal communication) for two upper air stations at Whenuapai ( $36.47^\circ\text{S}$ ,  $174.38^\circ\text{E}$ ) and Paraparaumu ( $40.54^\circ\text{S}$ ,  $174.59^\circ\text{E}$ ). Launches were made at approximately 0000 UTC and 1200 UTC on 17 June 1996. Figure 7 shows the vertical temperature profiles at Whenuapai locations at 0000 and 1200 UTC, 17 June. The vertical dotted lines on the plot indicate temperatures of  $-35^\circ\text{C}$  and  $-45^\circ\text{C}$ , which cover the range of opaque cloud top temperatures observed in the AVHRR image. These temperatures translate to heights of 7.5 to 8.5 km. Radiosonde data at Paraparaumu and data for the other days, give substantially the same results. Indeed it is sufficient to use the mean monthly profiles in this analysis, because the lapse rate is not varying strongly during this time in this height range of the atmosphere. (Note that this may not have been the case had the plume been higher, or lower, in the atmosphere.)

The plumes of 8 July observed in ATSR-2 and in AVHRR-2 imagery indicate that in the most opaque regions, the coldest parts of the cloud were  $-20^\circ\text{C}$  to  $-25^\circ\text{C}$ . These temperatures translate to cloud top heights of about 5 to 6 km.

### Cloud stereoscopy

Prata and Turner (1997) have developed an algorithm for determining cloud heights from the parallax formed between the ATSR forward and nadir views of clouds. The method is capable

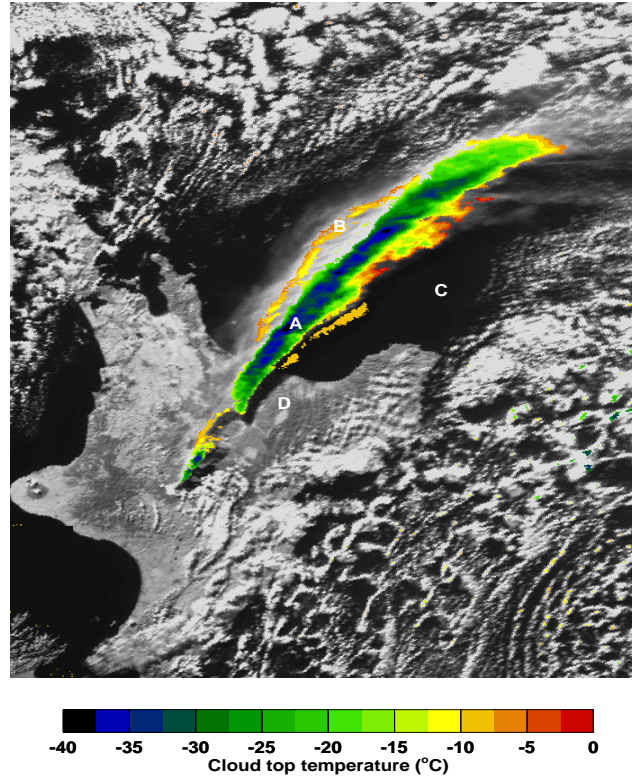


Figure 6. Brightness temperature ( $T_4$ ) for the Ruapehu plume of 17 June 1996.

of accuracies of  $\approx 1$  km in height and was used to determine plume height in the ATSR-2 image of 8 July. Figure 8 shows the plume at nadir (Fig. 8a) and in the forward view (Fig. 8b), using the  $1.61 \mu\text{m}$  channel. A point on the plume some distance downwind of the vent (marked by + on the Figures) and a point on the plume near to the vent (marked by X on the Figures) are used to illustrate the results. It is apparent that the same points are shifted by several lines in the forward view relative to the nadir view. For the points shown, the stereoscopic retrieval gives heights of  $\approx 7$  km for the downwind point, and 5.5 km for the point near to the vent (cf. heights of 5-6 km from the brightness temperature method). Height retrievals along the length of the plume suggest a slight rise of the plume from about 5 km near to the vent to about 8 km downwind.

### Height from plume shadow

The AVHRR-2 image of 17 June lends itself to a determination of plume height morphology from the shadow cast on the underlying surface. The method used to determine the plume height is applied separately for portions over the sea and over the land. We describe the analysis for deriving the plume height from the image of the plume and its shadow. The case of the shadow on the ocean is described first, then the more complicated case for the land.

Figure 9 shows the geometry when the shadow falls on the flat ocean. Define an  $x$ - $y$  coordinate

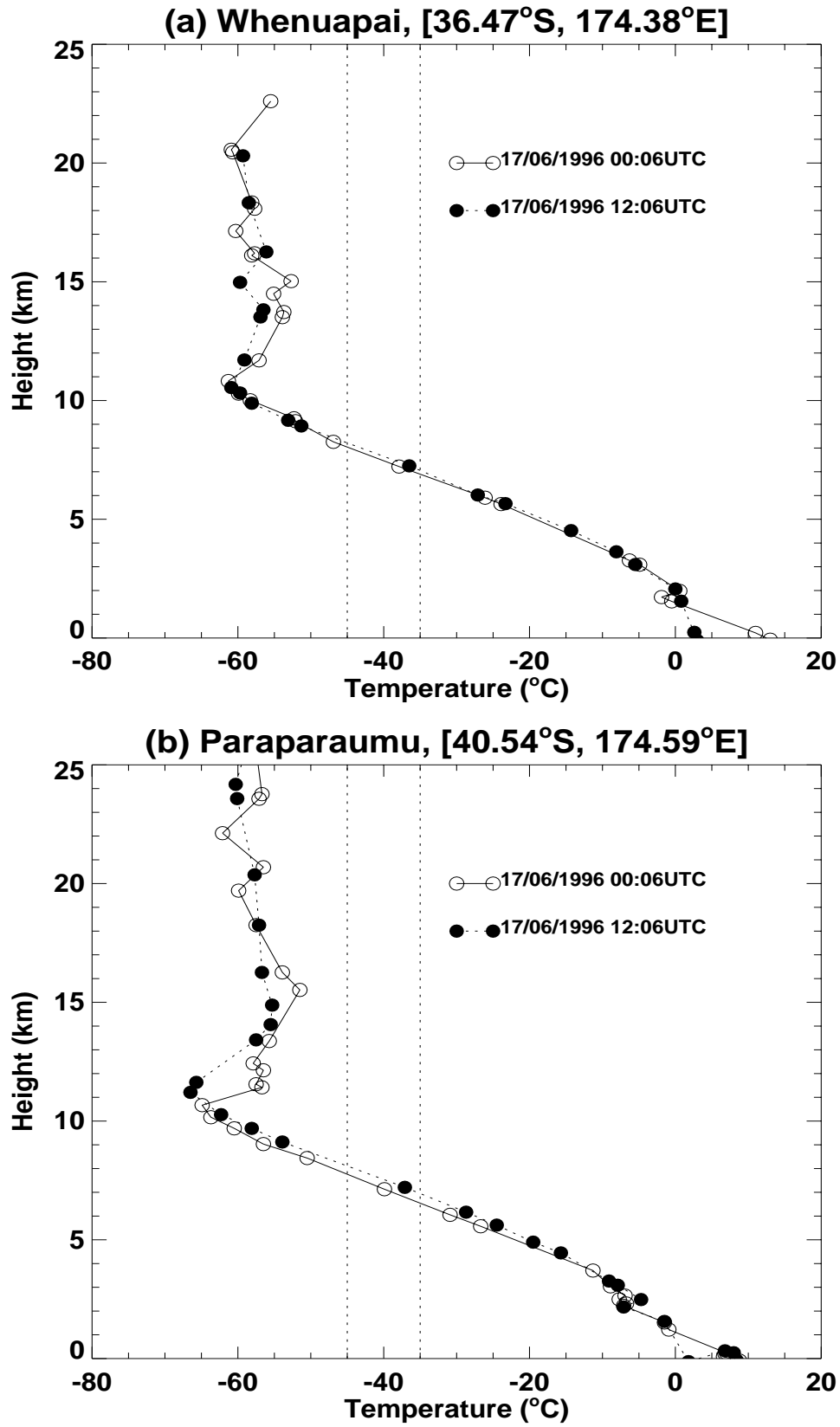


Figure 7. Radiosonde profiles.



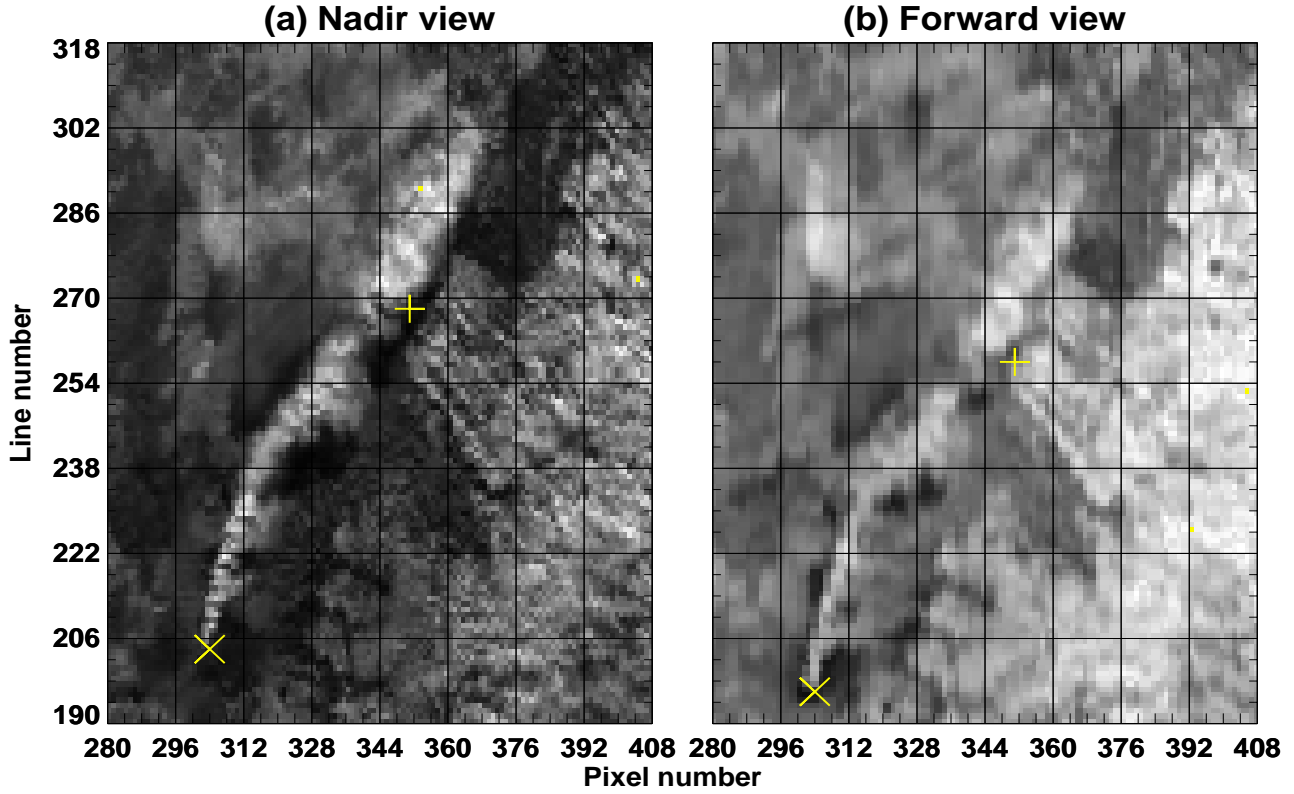


Figure 8. ATSR-2 stereoscopy. The *left panel* shows the nadir view of a portion of the Ruapehu plume. The *right panel* shows the corresponding plume in the forward view. Two points marked **X** and **+** are displaced in the forward view with respect to the nadir view.

system on the ocean surface with  $x$  north and  $y$  east, and consider a point  $T$  on the plume edge at altitude  $h$  above the origin. The direction of the satellite from  $T$  is described by the zenith angle  $\theta$  and the azimuth  $\phi$ , and the solar direction is given by angles  $\theta_0$  and  $\phi_0$ . Point  $T$  casts its shadow at point  $S$  on the surface, and the position of  $T$  in the image is actually that of its projection  $P$  along the satellite view direction to the surface.  $S$  and  $P$  have coordinates

$$\begin{aligned} x_S &= h \tan \theta_0 \cos(\phi_0 - \pi) \\ y_S &= h \tan \theta_0 \sin(\phi_0 - \pi) \\ x_P &= h \tan \theta \cos(\phi - \pi) \\ y_P &= h \tan \theta \sin(\phi - \pi). \end{aligned} \quad (12)$$

The vector  $\Delta$  from  $P$  to  $S$  has components

$$\begin{aligned} x_\Delta &= hX \\ y_\Delta &= hY, \end{aligned} \quad (13)$$

where

$$\begin{aligned} X &= \cos \phi \tan \theta - \cos \phi_0 \tan \theta_0 \\ Y &= \sin \phi \tan \theta - \sin \phi_0 \tan \theta_0. \end{aligned} \quad (14)$$

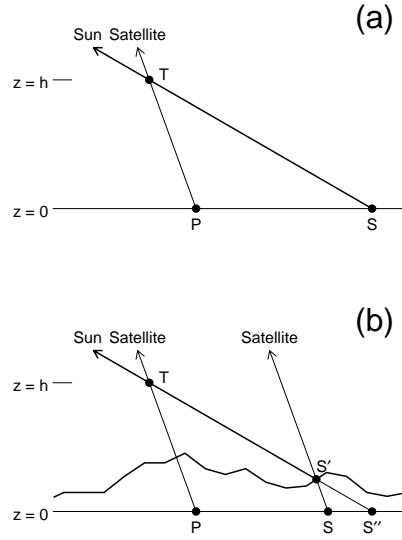


Figure 9. (a) The geometry over the ocean for a case where the view and sun directions are in the same vertical plane, depicted in that plane. (b) The geometry with the view and sun angles as in panel (a), but now over land.

The direction of  $\Delta$  is described by its azimuth

$$\phi_{\Delta} = \arctan \frac{Y}{X}, \quad (15)$$

and its magnitude is

$$d = h\sqrt{X^2 + Y^2}. \quad (16)$$

Because  $\phi_{\Delta}$  is independent of  $h$ , the association between points on the plume edge and points on the shadow edge in the image is straightforward; any point on the imaged plume edge is connected to its shadow point by a line with orientation  $\phi_{\Delta}$ . The true height of the plume edge is proportional to the separation of the plume and shadow edges along this line,

$$h = \frac{d}{\sqrt{X^2 + Y^2}}. \quad (17)$$

The analysis of the shadow on the ocean begins by rotating the image so that, for example, the  $y$ -direction is parallel to the azimuth  $\phi_{\Delta}$ . Then each column in the image is analyzed separately; the edge points of the plume and shadow images are found, then the relative three-dimensional coordinates of the true plume edge point determined by equations (17) and (13). At first we tried to set the plume and shadow edges at the local extrema of  $d(\log r)/dy$ , where  $r$  is the pixel radiance, but these positions were somewhat unstable, fluctuating along the plume.



(available at <http://www.ngdc.noaa.gov/mgg/global/seltopo.html>), which has 5-arcminute resolution.

Figure 11 shows a close-up channel 1 (visible) view of a part of the AVHRR-2 image of the Mt. Ruapehu plume obtained on 17 June 1996. Where the plume crosses the North Island of New Zealand there is a distinct darkening of the channel 1 reflectance. This shadow can also be detected over the ocean when the image data are suitably enhanced. Since time and position of each pixel are available it is straightforward to obtain the relevant solar and satellite viewing angles required to compute the height of the illuminated edge of the plume. The morphology of real plumes is likely to be quite complex and it is difficult to calculate the precise part of the cloud that is responsible for the shadow.

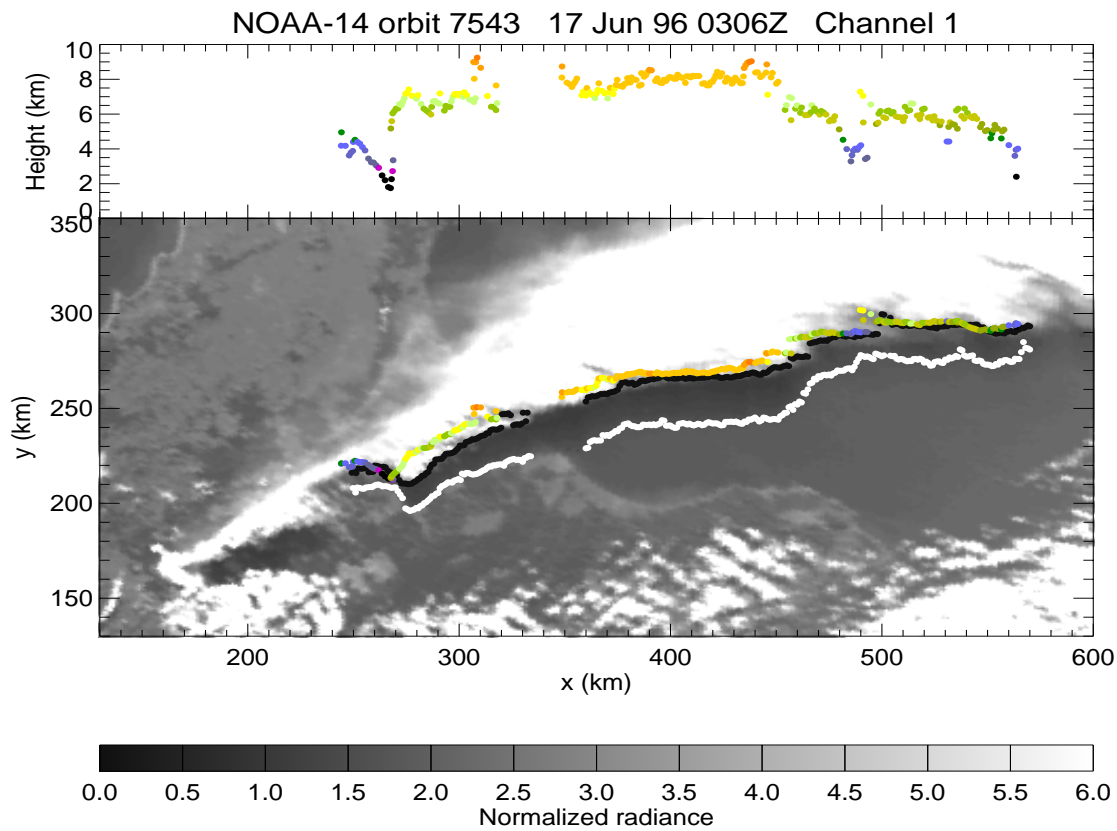


Figure 11. *Bottom panel:* The AVHRR channel 1 image, rotated so that the  $y$ -axis is in the azimuth  $\phi_{\Delta} = 153^{\circ}$  described in the text. The black points are taken as the plume edge (points  $P$  in the appendix) and the white points as the shadow edge (points  $S$ ). The coloured points show the vertical projection of the calculated true plume edge; that is, the plume edge where it would be imaged by a nadir-viewing satellite. The colours code the calculated height of the plume edge and represent the same height intervals as in the top panel. *Top panel:* The calculated height of the plume edge.

Figure 11 also shows the retrieval of height of the plume edge (top panel) and corresponding locations of the edge and its shadow as determined on the AVHRR-2 image. As described previously, the height retrieved by this method is, strictly speaking, that of the plume edge

(Glaze *et al.*, 1999). We expect this height to correspond more closely with the lower part of the plume, and represent a lower bound on the plume height and an upper bound on the plume base. The plume edge height varies from values as small as 2 km, up to just over 8 km, some 200 km downwind of the vent.

## **7 Water vapour corrections**

Water vapour has a differential absorption effect on the infrared window radiances so that at the top of the atmosphere the radiance (or brightness temperature) is larger at 11  $\mu\text{m}$  than at 12  $\mu\text{m}$ . This is the opposite to the absorption effect caused by volcanic ash and thus water vapour can ‘hide’ the ash effect. A method to correct for the water vapour effect, based on global radiative transfer simulations has been devised and is described here.

### **Global radiative transfer calculations**

Detailed radiative transfer calculations were performed using the MODTRAN-3 code to determine the top-of-the-atmosphere (TOA) brightness temperatures for the AVHRR, GMS-5, GLI and ATSR-2 split-window channels. The calculations utilised global NCEP analyses for four different days and two different times. The days and times were chosen to represent seasonal and diurnal variations in atmospheric water vapour conditions. Figure 12 shows the TOA brightness temperature at 11  $\mu\text{m}$  (top panel), the precipitable water amount (cm), and the temperature difference ( $T_4 - T_5$ ) between the 11  $\mu\text{m}$  and 12  $\mu\text{m}$  AVHRR split window channels. The calculations shown are for 26 December 1996 at 00Z. The most notable feature of these calculations is the high degree of spatial correlation between the fields of precipitable water and  $T_4 - T_5$ . There is a marked nonlinear relationship between the TOA brightness temperature and precipitable water. Similar results were found for the other days and times.

Water vapour amount is not distributed uniformly over the globe. Largest amounts are found in tropical and subtropical regions while the polar regions are relatively dry. Water vapour distributions also appear to follow weather systems and the patterns resemble the cloud patterns associated with frontal systems. There also appears to be a strong correlation between warm ocean current systems and high water vapour loadings. These general patterns in water vapour amount (or precipitable water) are reflected in the global patterns of AVHRR  $T_4 - T_5$ .

Results for the GMS-5, ATSR-2 and GLI are shown for comparison in the panels of Figure 13. There are minor differences between  $T_4 - T_5$  for the ATSR-2, GLI and AVHRR sensors, but major differences for the GMS-5 sensor. This is essentially due to the degree of overlap between the GMS-5 split window channels, which reduces the size of the  $T_4 - T_5$  difference for a given precipitable water amount.

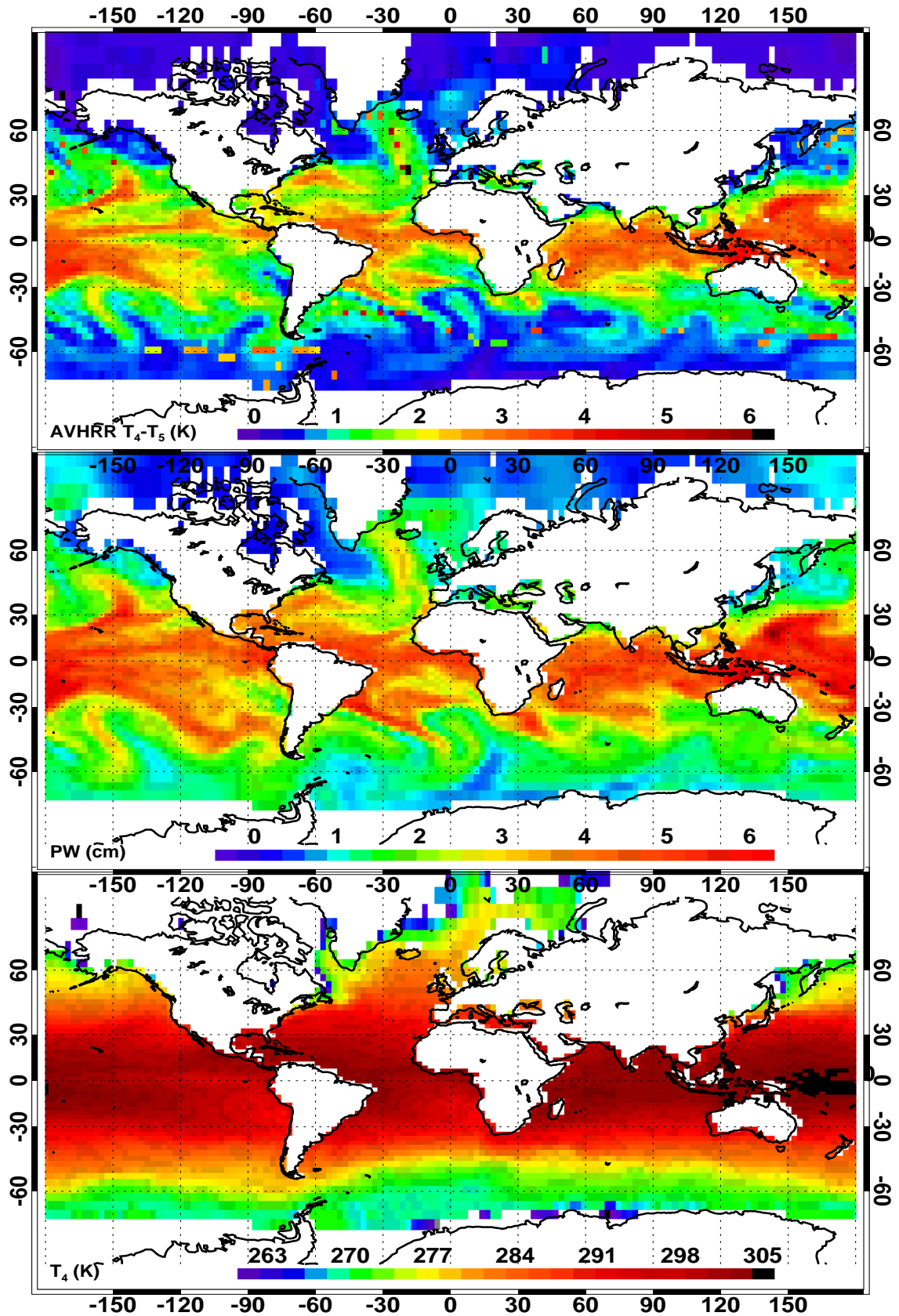


Figure 12. Global distributions of 11  $\mu\text{m}$  - 12  $\mu\text{m}$  brightness temperatures ( $T_4 - T_5$ , K; top panel) precipitable water (cm; middle panel) and 11  $\mu\text{m}$  brightness temperature (K; bottom panel) for 26 December 1996 at 00 Z.

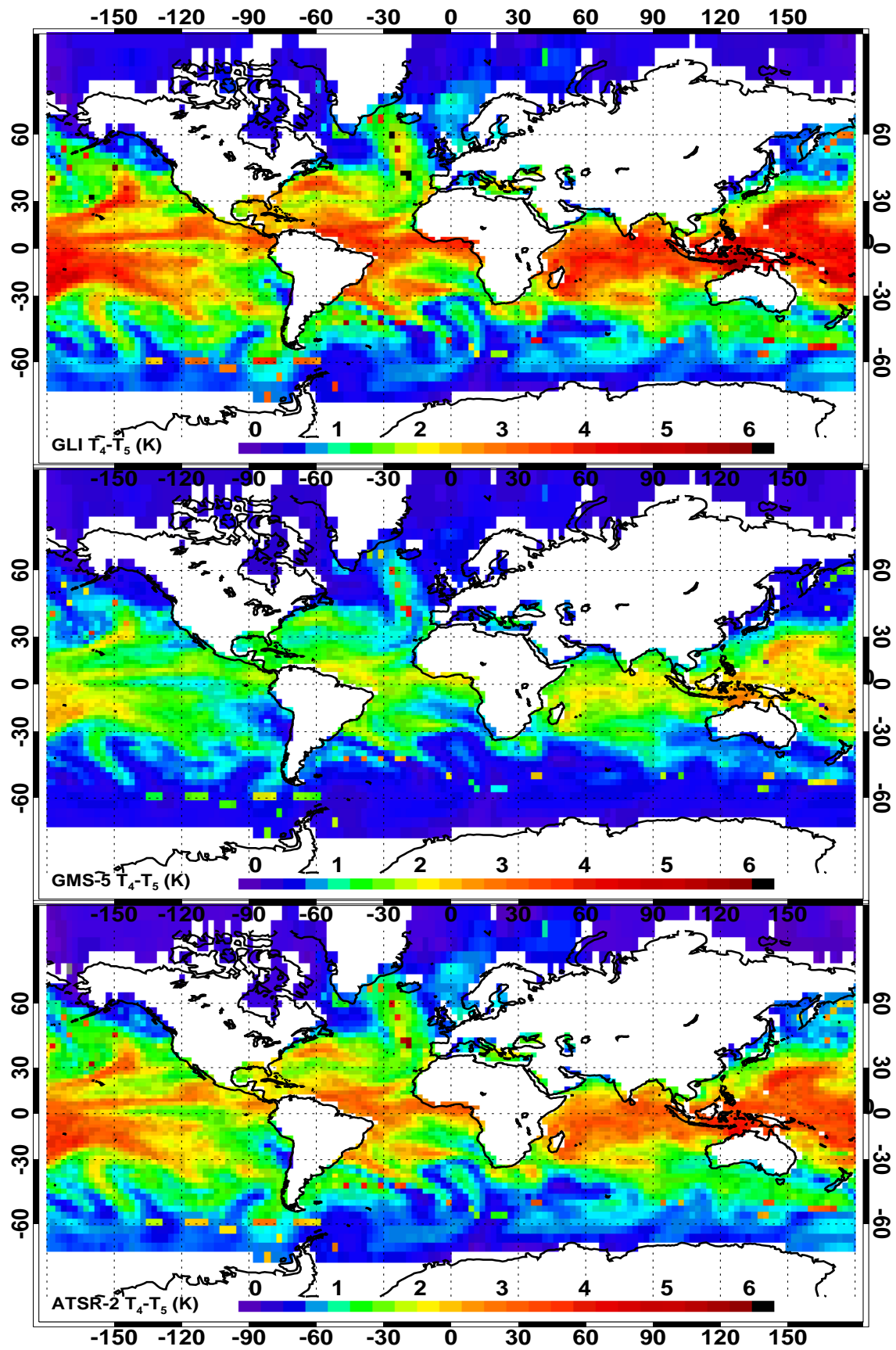


Figure 13. Global distributions of GLI 11  $\mu\text{m}$  - 12  $\mu\text{m}$  brightness temperatures ( $T_4 - T_5$ , K; top panel) GMS-5 (K; middle panel) and ATSR-2 (K; bottom panel) for 26 December 1996 at 00 Z.

## A semi-empirical water vapour correction

The RT calculations suggest that there is a very strong correlation between precipitable water and  $T_4 - T_5$  and a strong, but nonlinear correlation between precipitable water and top-of-the-atmosphere temperature at  $11\ \mu\text{m}$  or  $12\ \mu\text{m}$ . This latter nonlinear relation derives from the correlation between SST and precipitable water. Therefore there exists a nonlinear correlation between  $T_4 - T_5$  and  $T_4$  through precipitable water. This fact is no surprise as it is the basis for estimating SST from the AVHRR and other instruments relying on the split-window channels.

Figure 14 shows the correlations between precipitable water (in cm) and  $T_4 - T_5$ , and  $T_4$  and  $T_4 - T_5$  calculated using RT and the NCEP data described earlier.

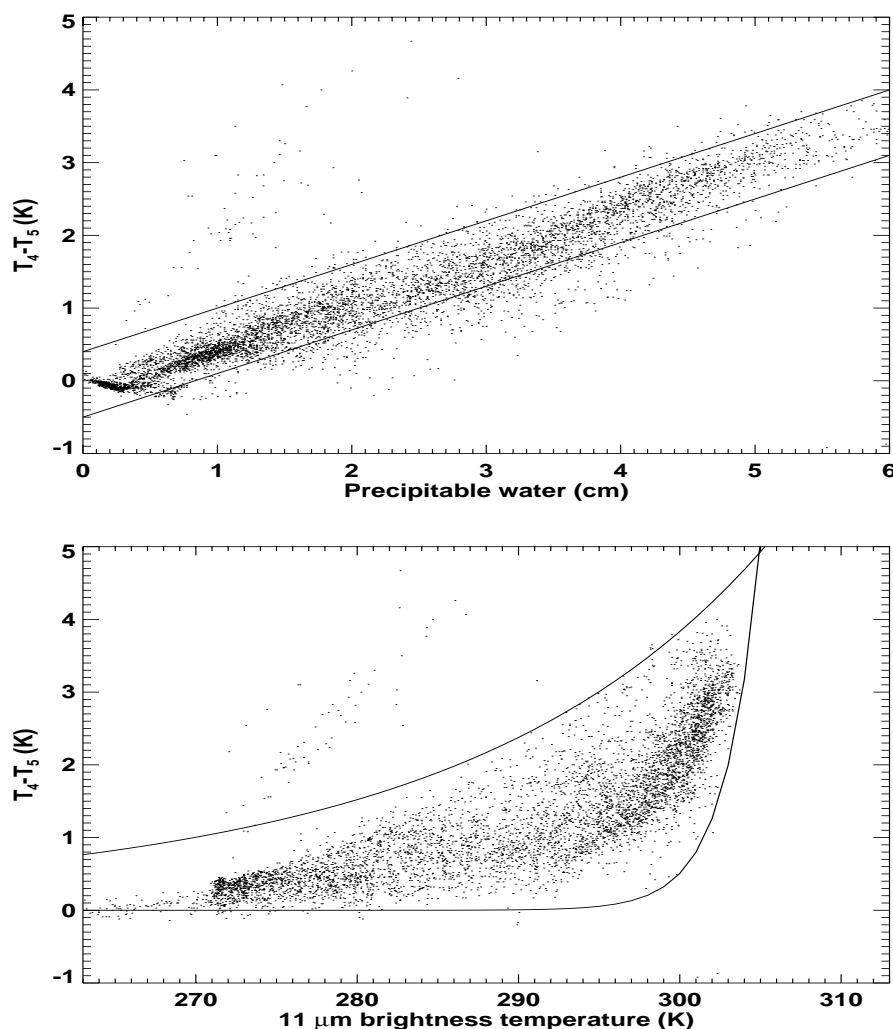


Figure 14. Global distributions of  $11\ \mu\text{m}$  -  $12\ \mu\text{m}$  brightness temperatures ( $T_4 - T_5$ , K; top panel) precipitable water (cm; middle panel) and  $11\ \mu\text{m}$  brightness temperature (K; bottom panel) for 26 December 1996 at 00 Z.



The data shown are for 26-12-1996 at 00Z, but very similar results are obtained for other dates and times. Also shown on Figure 12 are empirical fits providing upper and lower bounds to the distribution of the points. The semi-empirical relations describing these bounds are,

Upper bound:

$$\Delta T_{vv} = \exp [20T_* - 18] . \quad (18)$$

Lower bound:

$$\Delta T_{vv} = \exp [6T_* - b] , \quad (19)$$

where  $T_* = T_4/T_{max}$ , and  $T_{max}$  is an arbitrary normalisation constant assigned a value of 320 K. The free parameter  $b$  essentially determines the value of the water vapour effect on  $T_4 - T_5$  at the maximum value of  $T_4$ . Hence  $b$  can be determined directly from the image data, allowing realistic flexibility on the size of the water vapour correction determined by this semi-empirical approach.

### **Test case: Rindjani eruptions, Indonesia, June 1994**

The semi-empirical approach to water vapour correction for volcanic ash detection has been tested on some eruptions of Rindjani volcano on the island of Lombok in Indonesia. These eruptions were mostly low level and occurred in a moisture laden, tropical atmosphere. Detection using the reverse absorption effect was successful on many AVHRR images, but it is known from the work of Prata (1989a, b), Wen and Rose (1994), and Davies and Rose (1998) that water vapour will have the effect of suppressing the size of the negative differences. Thus a water vapour correction is warranted. Four test cases are shown in Figure 15, where distributions of  $T_4 - T_5$  vs.  $T_4$  are plotted without a water vapour correction (black points), and with a water vapour correction (red points).

The continuous line is a simplified model of the behaviour of  $\Delta T$  for volcanic ash clouds described by Prata and Grant (2000) and developed from radiative transfer considerations. The model may be written:

$$\Delta T = \Delta T_s [X - X^\beta], \quad (20)$$

where,

$$X = 1 - \frac{\Delta T_s}{\Delta T_4},$$

$$\Delta T_4 = T_4 - T_c,$$

$$\Delta T_s = T_s - T_c,$$

and the cloud-top and surface temperatures are  $T_c$  and  $T_s$ . The parameter  $\beta$  links the spectral behaviour of the top-of-the atmosphere brightness temperatures ( $T_4, T_5$ ) to the cloud micro-physics, through the ratio of spectral extinction efficiencies for volcanic ash. Mie calculations by Prata (1989b) and Prata and Barton (1994) for silicate spherical particles suggest values of  $\beta$  from  $\approx 0.6$  to  $\approx 0.86$ . A value of  $\beta=0.71$  was used in Figure 15.

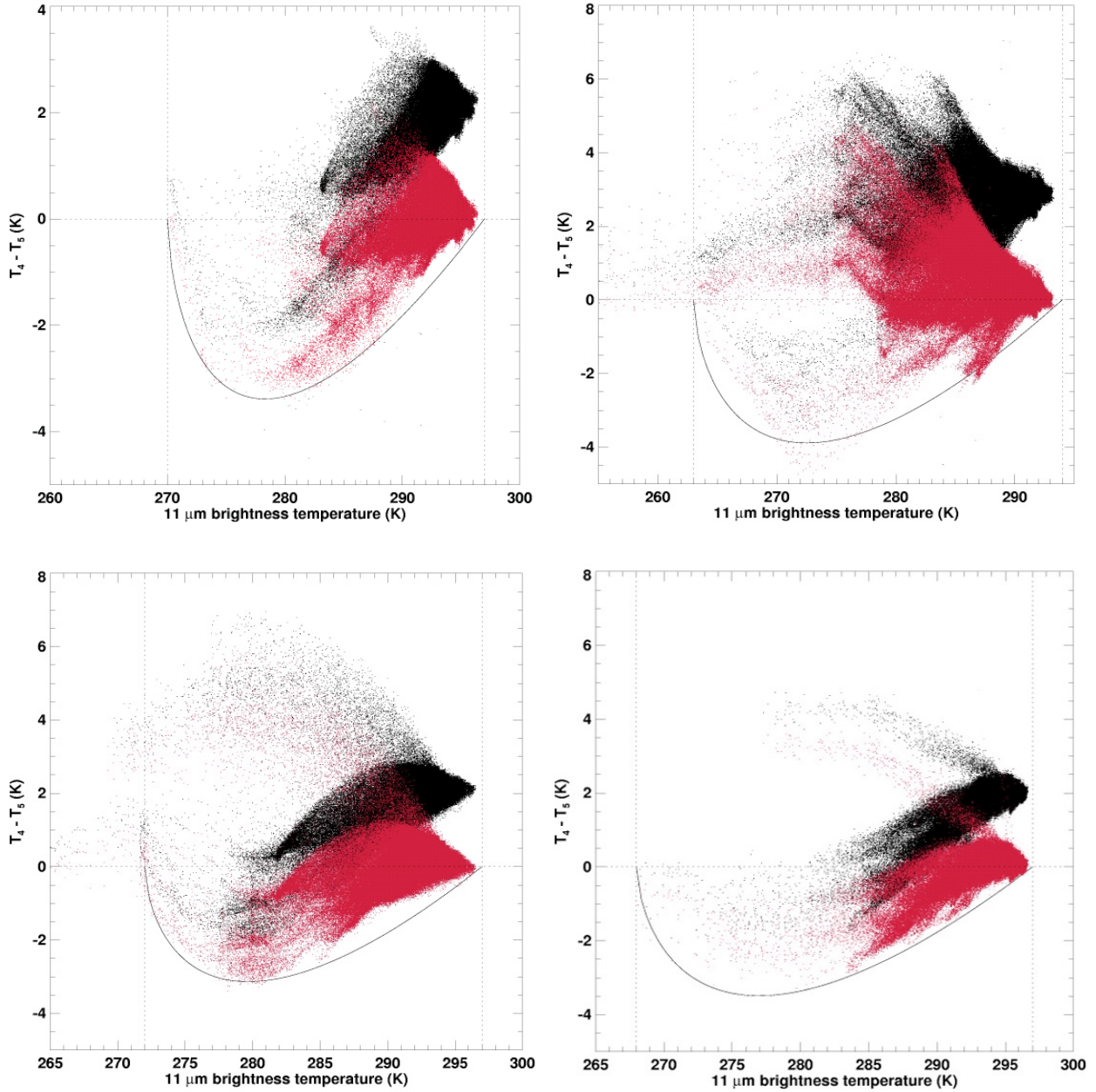


Figure 15. Temperature difference distributions without (black dots) and with (red dots) a water vapour correction for four different eruption clouds from Rindjani, Indonesia.

Theory suggests values of  $\Delta T < 0$  are ash, but this does not take into account measurement errors, primarily resulting from instrument noise, poor calibration and channel misregistration. The water vapour correction and the theory utilised are also approximations and contain some degree of uncertainty. Each pixel is likely to contain a mixture of water vapour and ash. We assume that the temperature difference observed arises from a linear combination of the signal from ash ( $\Delta T_{ash}$ ) and the signal from an otherwise clear pixel, any temperature difference being due to water vapour ( $\Delta T_{wv}$ ). If the fraction of ash in the mixture is  $F$ , then we may write the observed temperature difference as,

$$\Delta T = F \Delta T_s [Z - Z^\beta], \quad (21)$$

where,

$$Z = 1 - \frac{1}{F} \frac{\Delta T_4}{\Delta T_s},$$

The other parameters are defined as before. Ideally this procedure needs to be automated. There are several parameters that can be determined from the image data. These are:

(1) the clear-sky surface temperature  $T_s$ , (2) the cloud-top temperature  $T_c$ , (3) the clear-sky value of the water vapour correction, parametrised by  $b$ , and (4) the ratio of extinction coefficients  $\beta$  that governs the magnitude of the “U”-shaped distribution of negative differences.

A procedure for estimating these parameters from the image data has been developed. A brief outline is given below.

1.  $T_s$ . This is easily estimated by finding the maximum value of  $T_4$  occurring in the data. A component for water vapour absorption correction is added using the method described earlier.
2.  $T_c$ . This is more difficult to estimate from the data, because the lowest value may not necessarily correspond to the volcanic cloud. However, provided an area in close proximity to the suspect cloud can be delineated it may be reasonable to assume that the lowest value is the cloud-top temperature.
3.  $b$ . This is estimated by evaluating  $T_4 - T_5$  for the pixel corresponding to the maximum value of  $T_4$ . Then (2) is solved for  $b$ . Values of 3 to 5 appear to be acceptable.
4.  $\beta$ . Theoretical estimates of  $\beta$  suggest a value of around 0.7. A method for estimating  $\beta$ ,  $T_s$  and  $T_c$  simultaneously has been developed by using the distribution of  $T_4$  vs  $T_4 - T_5$ . The distribution is first histogrammed (or binned) into intervals of 0.5 K in  $T_4$ . Then, the lowest values in each bin are found and a curve is generated giving the outline of the distribution. The curve is smoothed and fitted using a nonlinear least squares model. The model has three parameters, viz.:  $T_s$ ,  $T_s - T_c$  and  $\beta$  that can be estimated from the fit.

The curve-fitting procedure uses the model developed earlier with  $F = 1$  and the partial derivatives of the model, which are analytic. Writing,

$$Y = \alpha(X - X^\beta),$$

where,  $Y = T_4 - T_5$ ,  $\alpha = T_s - T_c$ ,  $X = 1 - \frac{\gamma}{\alpha}$ ,  $\gamma = T_s - T_4$ . The partial derivatives are,

$$\frac{\partial Y}{\partial \alpha} = (X - X^\beta) + \frac{\gamma}{\alpha} + \beta \frac{\gamma}{\alpha} \left(1 - \frac{\gamma}{\alpha}\right)^{\beta-1},$$

$$\frac{\partial Y}{\partial \beta} = \alpha X^\beta \text{Log} \beta,$$

$$\frac{\partial Y}{\partial \gamma} = 1 - \beta X^{\beta-1}.$$

An example of the curve-fitting procedure is shown in Figure 16. The distribution shown is for a volcanic ash plume from the 1996 June eruption of Ruapehu, New Zealand. The solid green-coloured lines are isolines of constant ash fraction  $F$ , and the red dots show the extrema of the distribution estimated from the data at constant temperature intervals. The extrema are used as input to Eq. (21) to determine the parameters of the model for  $F=1.0$ . Once these parameters are determined,  $F$  can be inferred for all pixels in the distribution.

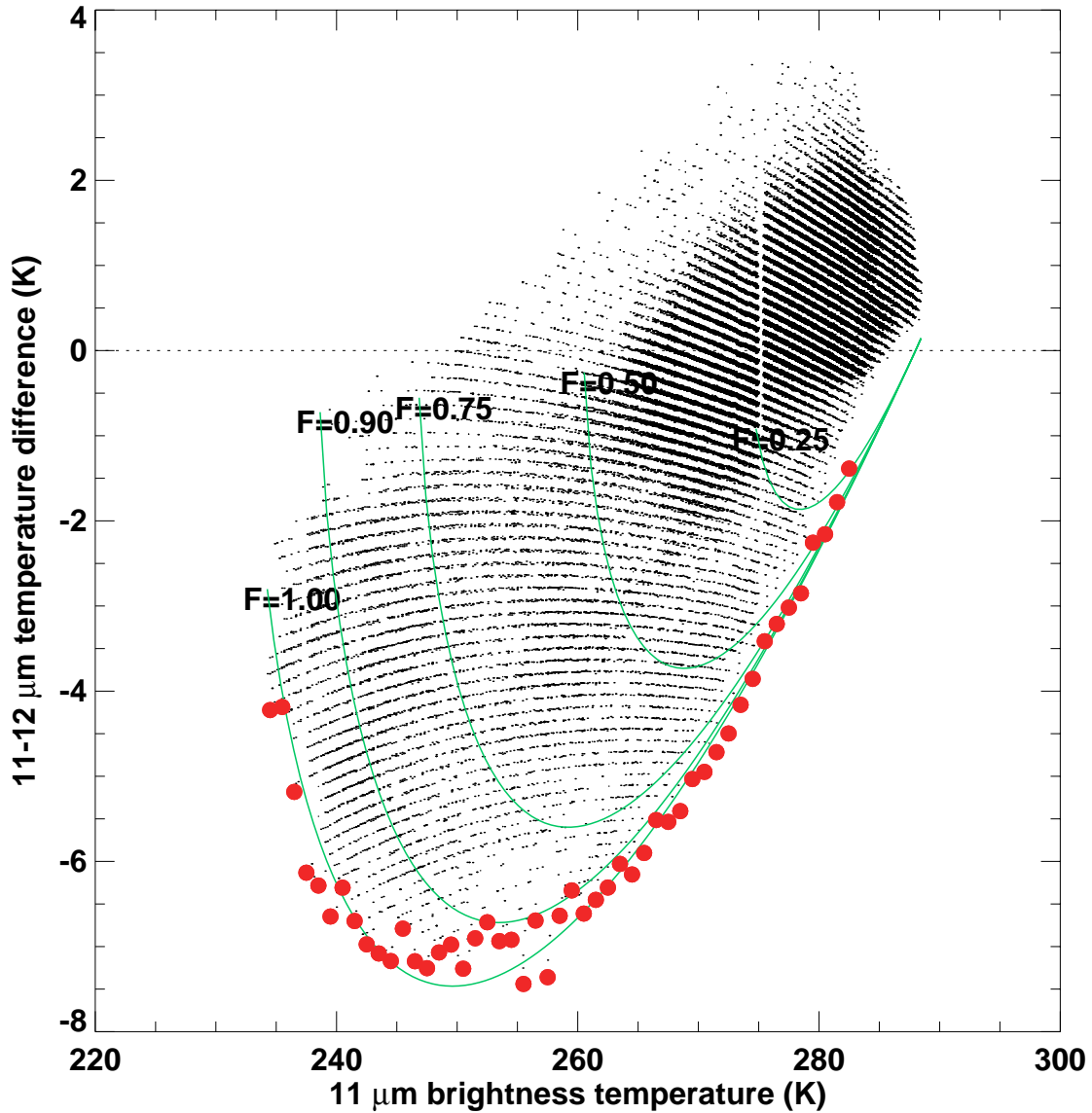


Figure 16. Distribution of  $T_4 - T_5$  for an eruption of Ruapehu volcano. The green-coloured lines are isolines of the fraction of ash determined from Eq. (21). The red dots are estimates of the extrema of the distribution derived from the data.

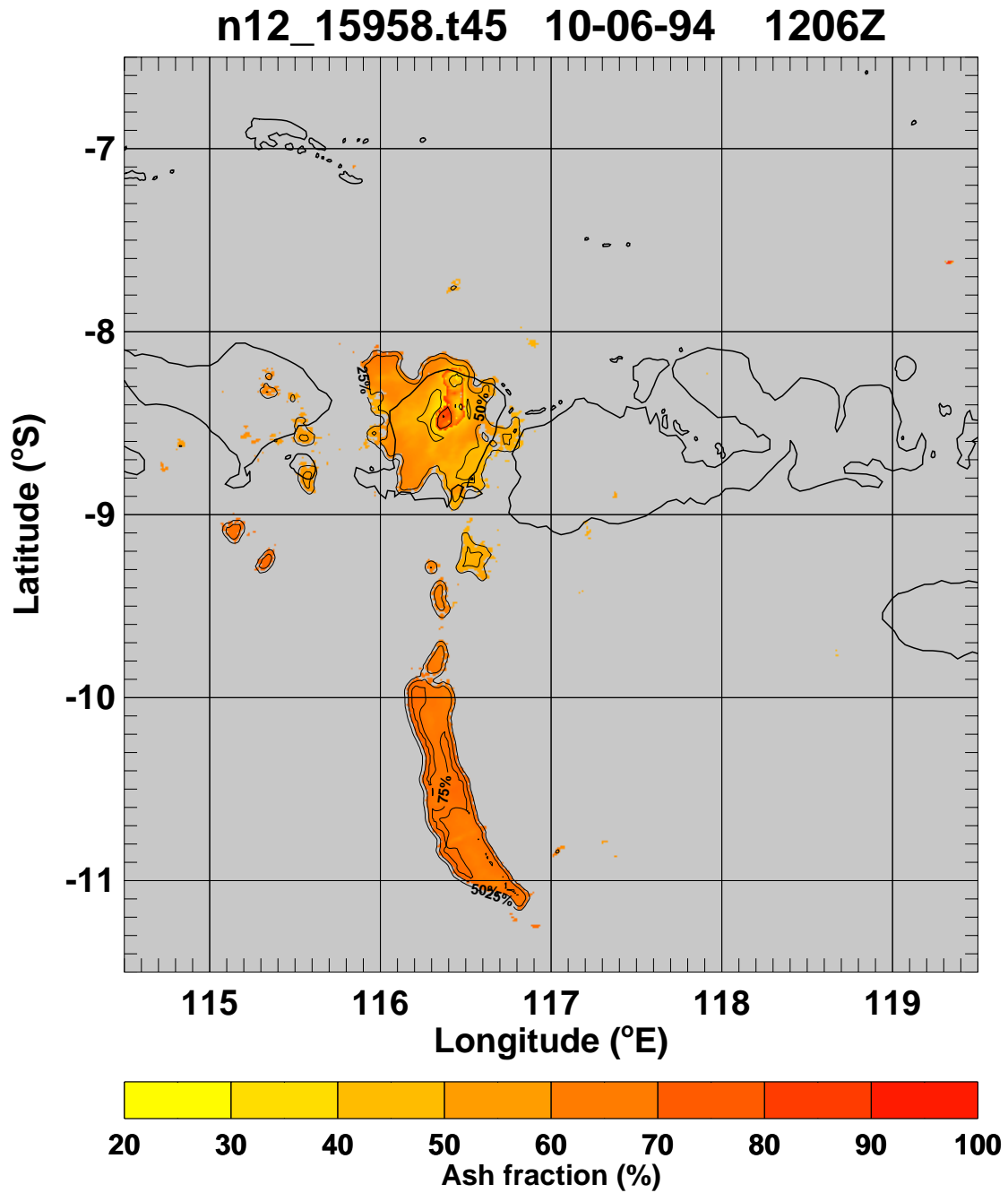


Figure 17. Ash fraction retrievals for eruption of Rindjani volcano, Indonesia. The colours and contours show the percentage of ash determined for each AVHRR pixel, assuming that the pixel contains a linear mixture of ash and water vapour components.

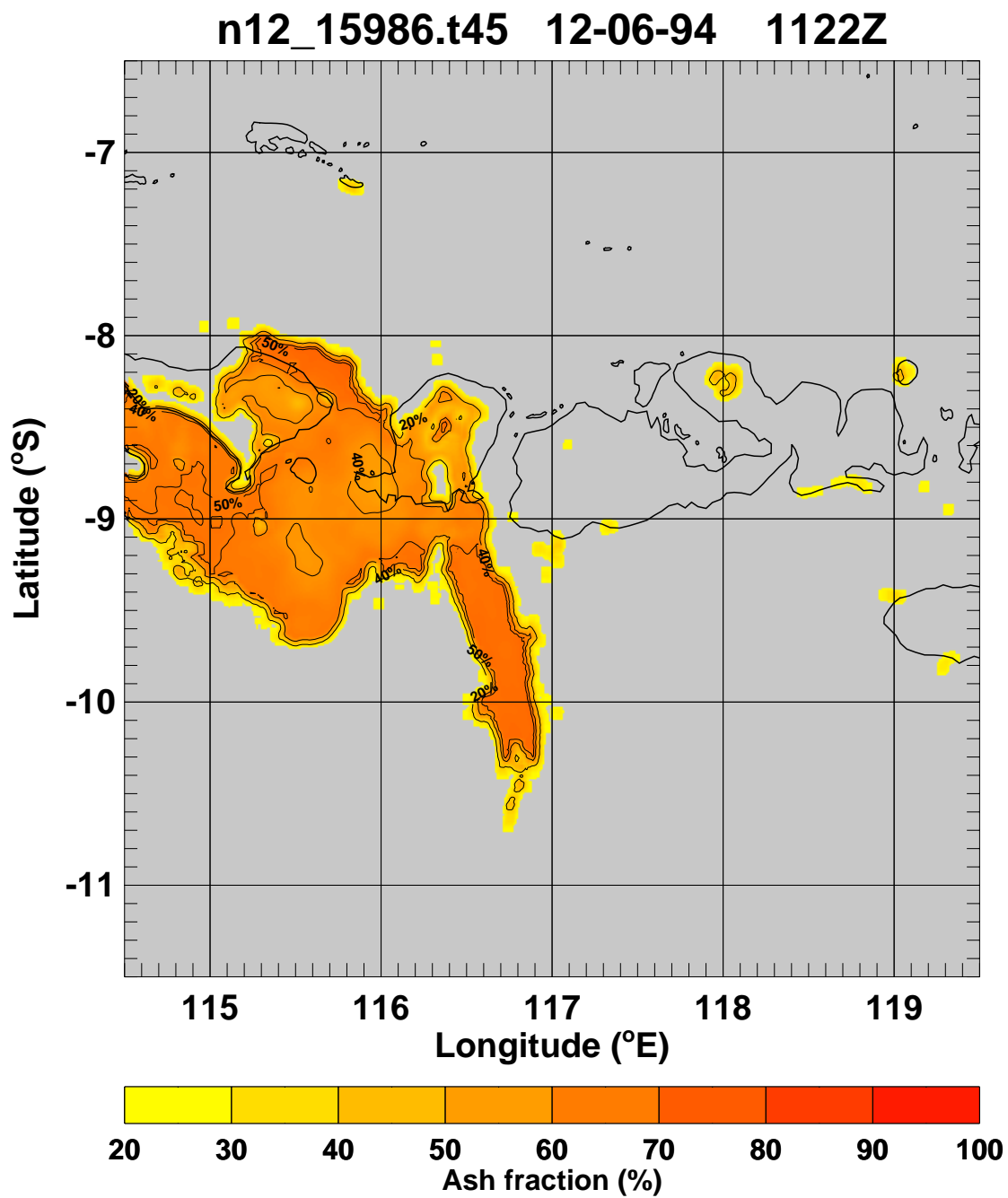


Figure 18. As for Fig. 17.

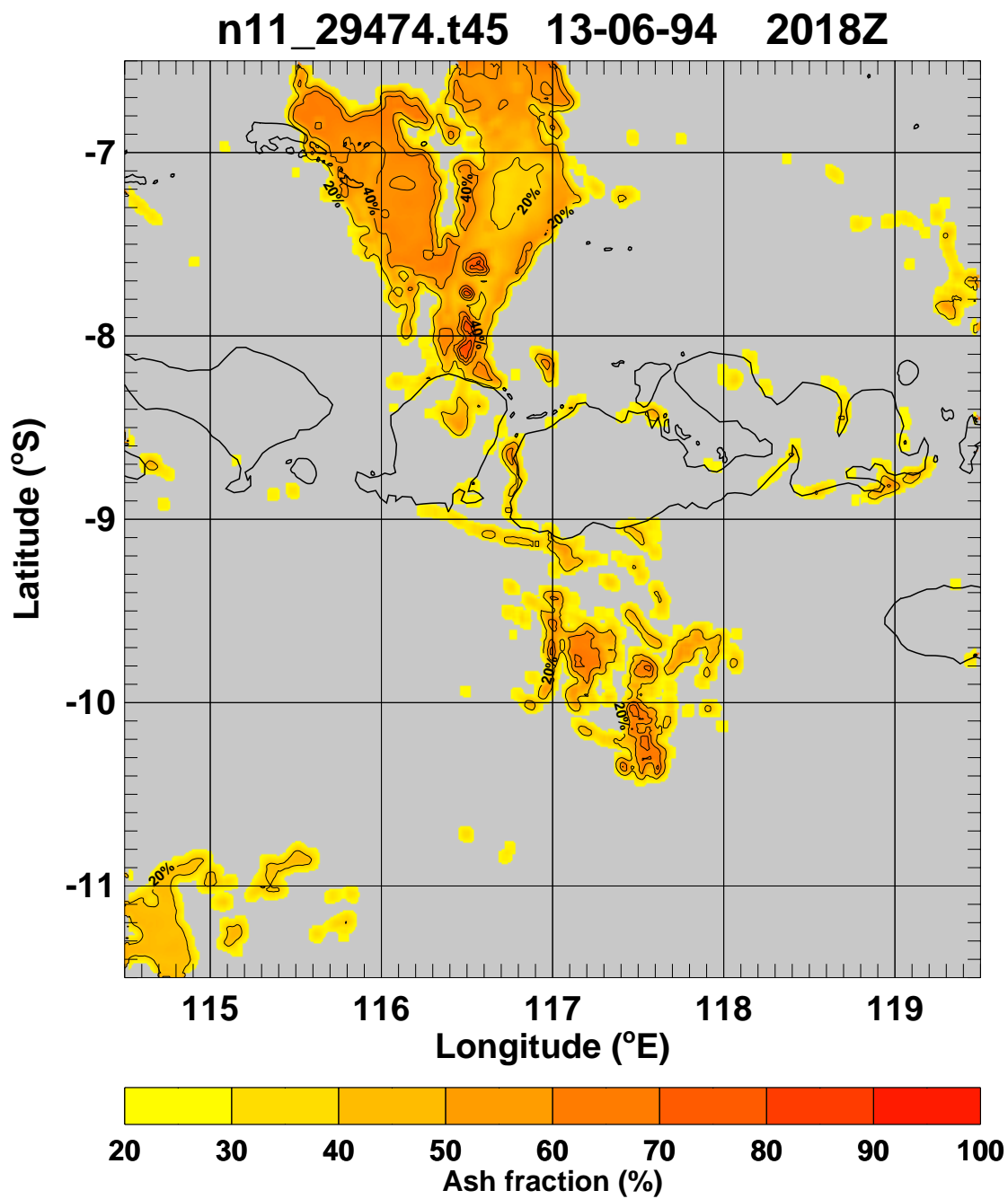


Figure 19. As for Fig. 17.

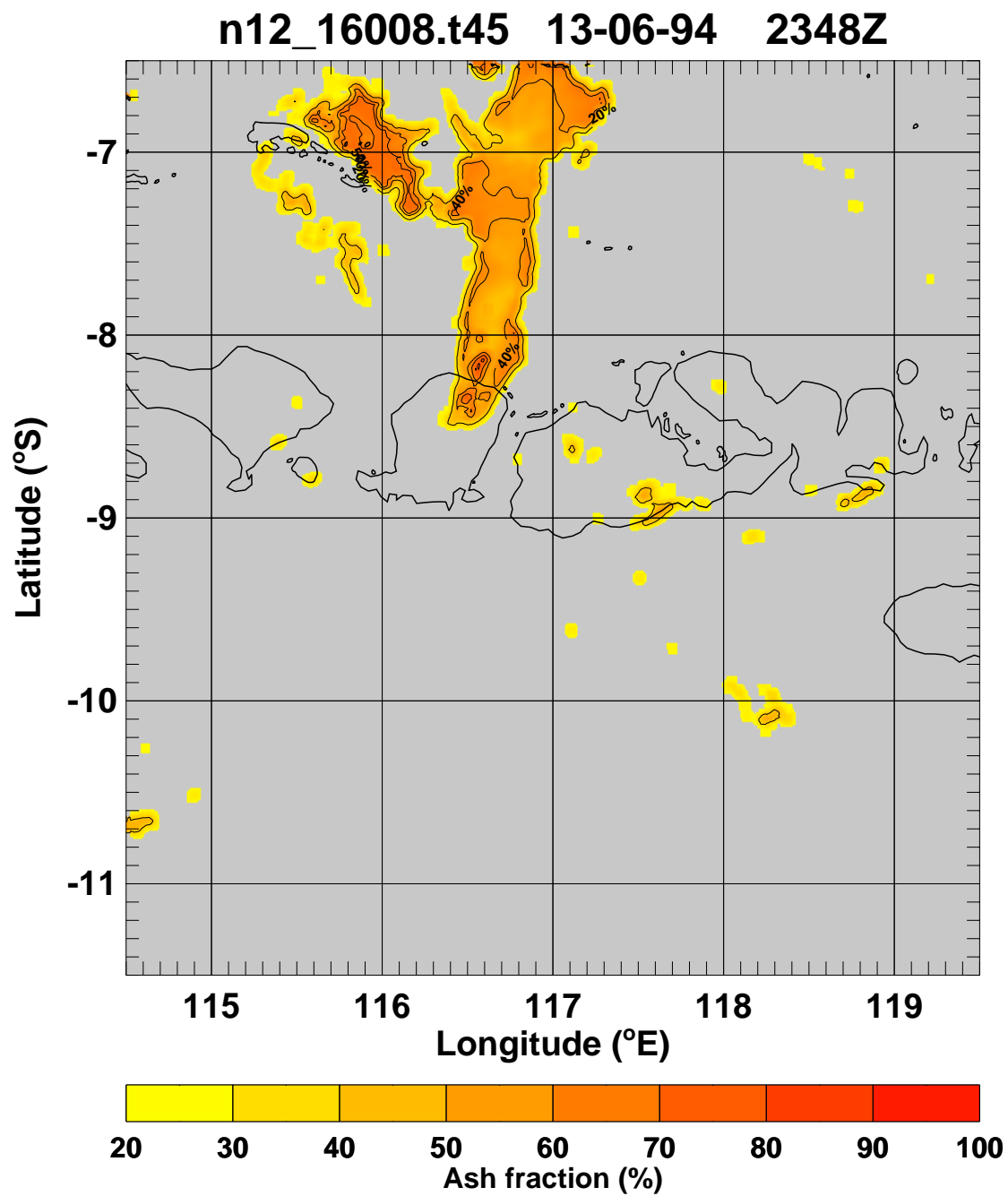


Figure 20. As for Fig. 17.



The ash fraction maps are an improvement over temperature difference images, but still suffer from ambiguities over land at night due to spectral emissivity effects for land surfaces. These can be overcome using a modified correction scheme that accounts for these spectral effects over the land. The correction simply allows for a lower emissivity at 11  $\mu\text{m}$  than at 12  $\mu\text{m}$  for pixels identified as land (using a map data-base) and have been applied to the nighttime images. Further improvements are likely by utilising a land cover scheme that identifies land pixels by their vegetation cover.

Another approach to water vapour correction is described by Yu *et al.* (2001). It is likely that many improvements in ash detection algorithms will be made in the coming years, especially with the advent of the new generation multispectral imagers.

## **8 Conclusions**

A retrieval scheme for deriving the mean particle radius of fine particles, the optical depth and cloud-top height and mass loadings of volcanic clouds using infrared satellite data has been described. The scheme was tested using data from eruptions of the Ruapehu volcano in New Zealand. The optical parameters required to perform the retrievals are provided in tabular form in this report for wavelengths ranging from the visible to the thermal infrared.

Currently, there are just a few satellite-borne sensors that can take advantage of these parameters, but the advanced sensors, AATSR/MERIS, MODIS, GLI and SEVIRI will have multiple wavebands in the visible, near-infrared and thermal that may be used to exploit this new information. Table 4 lists the wavebands of these sensors and highlights which channels may be of the greatest use for volcanic ash retrievals.

The report also provides a scheme for correcting infrared data for the effects of water vapour and the methodology is illustrated using satellite data for some eruptions of Rindjani volcano in Indonesia.

Finally, in conjunction with the results reported in Prata and Grant (2001), this report should provide forecasters at Volcanic Ash Advisory Centres (VAACs) concerned with hazards to aviation new means for improving their warnings.

Table 4: Central wavelengths and bandpasses of the advanced sensors GLI, AATSR/MERIS, MODIS and SEVIRI. Channels likely to be useful for volcanic ash detection are in bold.

<i>Central wavelength (<math>\mu\text{m}</math>)</i>		<i>Bandpass (<math>\mu\text{m}</math>)</i>		<i>Constituent detected</i>
GLI	AATSR/MERIS	MODIS	SEVIRI	
<i>Visible</i>				
0.375		—	—	—
0.400		—	—	—
0.412	0.412	0.405–0.420	—	—
0.443	0.442	0.438–0.448	—	—
0.460		—	—	—
0.490	0.490	0.483–0.493	—	—
0.520	0.510	0.526–0.536	—	—
0.545		0.546–0.556	—	—
0.565	0.560	—	0.56–0.71	—
0.625	0.620	—	0.56–0.71	—
0.667	0.665	0.662–0.672	0.56–0.71	—
<b>0.678</b>	<b>0.681</b>	<b>0.673–0.683</b>	<b>0.56–0.71</b>	<b>Ash</b>
0.710	0.705	—	—	—
0.748	0.754	0.743–0.753	0.74–0.88	—
0.763	0.760	—	0.74–0.88	—
	0.775	—	0.74–0.88	—
0.865	0.865	0.862–0.877	0.74–0.88	—
	0.890	0.890–0.920	—	—
	0.900	0.915–0.965	—	—
<i>Near infrared</i>				
1.05		—	—	—
1.10		—	—	—
1.24		1.230–1.250	—	—
1.37		1.360–1.390	—	—
<b>1.64</b>	<b>1.61</b>	<b>1.628–1.652</b>	<b>1.50–1.78</b>	<b>Ash</b>
2.21		2.105–2.155		—
<i>Thermal infrared</i>				
<b>3.72</b>	<b>3.73</b>	<b>3.660–3.840</b>	<b>3.48–4.36</b>	<b>SO<sub>2</sub>, Ash</b>
6.70			5.35–7.15	—
<b>7.00</b>			<b>6.85–7.85</b>	<b>SO<sub>2</sub></b>
<b>7.30</b>			<b>6.85–7.85</b>	<b>SO<sub>2</sub></b>
<b>8.30</b>			<b>8.30–9.10</b>	<b>SO<sub>2</sub>, H<sub>2</sub>SO<sub>4</sub>, Ash</b>
—	—	—	9.38–9.94	
<b>10.8</b>	<b>10.8</b>		<b>9.80–11.80</b>	<b>H<sub>2</sub>SO<sub>4</sub>, Ash</b>
<b>12.0</b>	<b>12.0</b>		<b>11.00–13.00</b>	<b>H<sub>2</sub>SO<sub>4</sub>, Ash</b>
—	—	—	<b>12.40–14.40</b>	<b>Ash</b>

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*Appendix. List of acronyms*

AATSR–*Advanced Along-Track Scanning Radiometer*  
ATSR–*Along-Track Scanning Radiometer*  
AVHRR–*Advanced Very High Resolution Radiometer*  
CRI–*Crown Research Institute*  
CSIRO–*Commonwealth Scientific and Industrial Research Organisation*  
DEM– *Digital Elevation Model*  
ENVISAT–*Environmental Satellite*  
ERS–*European Remote-sensing Satellite*  
GIFTS–*Geostationary Imaging Fourier Transform Spectrometer*  
GLI–*Global Imager*  
GMS–*Geostationary Meteorological satellite*  
GOES–*Geostationary Operational Environmental Satellite*  
GVN–*Global Volcanism Network*  
MERIS–*Medium Resolution Imaging Spectrometer*  
MIPAS–*Michelson Interferometer for Passive Atmospheric Sounding*  
MODIS–*Moderate resolution Imaging Spectroradiometer*  
MTSAT–*Meteorological Satellite*  
NOAA–*National Oceanographic and Atmospheric Administration*  
SEVIRI–*Spinning Enhanced Visible Infrared Imager*  
VAAC–*Volcanic Ash Advisory Centre*

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